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1 Effect of particle size on the dispersion behavior of magnesium stearate blended with 2 microcrystalline cellulose

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11 Abstract:

12 The majority of tablets manufactured contain lubricants to reduce friction during ejection. However,
13 especially for plastically deforming materials, e.g., microcrystalline cellulose (MCC), the internal
14 addition of lubricants is known to reduce tablet tensile strength. This reduction is caused by the surface
15 coverage by lubricant particles, the extent of which depends on both process and formulation parameters.
16 Previously published models to predict the lubrication effect on mechanical strength do not account for
17 changes in the excipient particle size. In this study, the impact of both lubricant concentration and mixing
18 time on the tensile strength of tablets consisting of three different grades of MCC and four grades of
19 magnesium stearate (MgSt) was evaluated. By taking into account the particle size of the applied
20 excipients, a unifying relationship between the theoretically estimated surface coverage and
21 compactibility reduction was identified. Evaluating the dispersion kinetics of MgSt as a function of time
22 reveals a substantial impact of the initial surface coverage on the dispersion rate, while the minimal
23 tensile strength was found to be comparable for the majority of formulations. In summary, the presented
24 work extends the knowledge of lubricant dispersion and facilitates the reduction of necessary
25 experiments during the development of new tablet formulations.

26 **Keywords:** tableting, magnesium stearate, lubrication, dispersion behavior, particle size

27 1. Introduction

28 The majority of industrial tablet formulations contain particulate lubricants, which facilitate tablet
29 ejection by reducing the interfacial friction between the lateral tablet surface and inner die wall.
30 However, the internal addition of lubricants is known to bear the risk of reducing the mechanical tablet
31 strength [1–5]. The reduction in mechanical strength is caused by the coverage of the surfaces of matrix-
32 forming diluent particles with lubricant particles [5,6]. The extent of mechanical strength reduction
33 strongly depends on the deformation behavior of the lubricated material [1]. Plastically deforming
34 materials are especially sensitive to lubrication, as they typically generate only a limited amount of fresh,
35 unlubricated surfaces during compaction [7,8]. Thus, the coverage of diluent surfaces by lubricant
36 particles may critically affect the interparticulate interactions if excessive amounts of lubricants are
37 added. In contrast, brittle fracturing excipients generate substantial amounts of new particle surfaces
38 during compaction, which explains their insensitivity towards lubrication with regard to their
39 mechanical tablet strength [9,10]. Generally, produced tablets must exhibit sufficient mechanical
40 strength to enable successful subsequent processing (such as transport, coating, and packaging) into
41 commercial medicines [11]. Consequently, for plastically deforming materials, in-depth knowledge of
42 the correlation between lubricant surface coverage and mechanical tablet strength is necessary to reduce
43 the number of time- and cost-intensive experiments during the development of new tablet formulations.

44 It is generally agreed that the detrimental effect of lubricant addition on mechanical strength is based on
45 the surface coverage by lubricant particles [5,6,12–14]. There has been a substantial effort to

46 characterize the underlying mechanisms and extent of surface coverage by lubricant particles
47 experimentally using different measurement techniques.

48 The majority of studies focused on the investigation of the distribution of magnesium stearate (MgSt),
49 which is the predominantly applied pharmaceutical lubricant. Initial studies applied scanning electron
50 microscopy (SEM) to investigate the distribution of MgSt on surfaces, which showed a sufficient
51 contrast to identify MgSt particles [5,6]. By combining SEM and energy dispersive X-ray analysis, the
52 surface coverage of NaCl [12] and API crystals [15] was quantitatively evaluated. Additionally,
53 secondary ion mass spectrometry [16] and raman spectroscopy [17] were found to be suitable to quantify
54 the distribution of MgSt. All these methods have in common that the determination of surface coverage
55 by lubricant particles is experimentally very laborious and has therefore only been carried out for
56 selected substance combinations in order to elucidate fundamental mechanisms.

57 Generally, the extent to which the lubricant addition affects tablet properties depends on the type of
58 applied lubricant [18–20], the lubricant amount [1,20], the lubricant particle size [21], the applied mixing
59 device [4,22], the mixing time [2,13] and, if applied, the paddle feeder passage [23–25]. The high
60 number of influencing factors and their complex interplay hinders, so far, the development of generally
61 applicable models that are capable of precisely predicting the impact of lubrication on the final tablet
62 tensile strength. Thus, previous research has been focused on developing suitable methods to
63 characterize individual sub-processes.

64 The most prominent model to capture the effect of lubrication on tablet strength was introduced by
65 Kushner et al. [4,26,27]. They developed a mathematical model that allows for scaling-up the mixing
66 process for lubricated formulations in free-fall mixers by taking into account the effects of several
67 process parameters (blender volume, headspace, and number of blender revolutions). However, as
68 pointed out by the authors themselves, their model is not able to capture the effect of changes in the
69 formulation. Thus, if the formulation is altered, time-consuming experiments to reparametrize the model
70 are necessary, which are economically unfavorable.

71 The effect of lubricant concentration on the reduction of compactibility was recently quantitatively
72 modeled by our research group by introducing an empirical model for binary formulations [28].
73 Subsequently, the model was combined with the model of Reynolds et al. [29] and, by that, extended to
74 more complex formulations [30]. The effect of lubricant concentration on structural and mechanical
75 tablet properties was modeled by theoretically estimating the surface coverage based on the initial
76 particle size distributions of applied excipients. However, the experiments were limited to very short
77 mixing times in a given blender setup, and by that, only a limited process setup was investigated.
78 Generally, it would be desirable to extend the available formulation knowledge in order to predict the
79 extent to which the mechanical strength is altered if one excipient is replaced with another grade
80 exhibiting a different particle size.

81 Therefore, in this study, a comprehensive evaluation of the mechanical strength of binary tablets
82 consisting of MCC and MgSt of different particle sizes for various lubricant concentrations and mixing
83 times was performed. By calculating the theoretical surface coverage of MCC particles by lubricant
84 particles, a unifying relationship between theoretical surface coverage and compactibility reduction due
85 to lubrication independent of the applied excipient particle size was derived for short mixing times.
86 Afterwards, for a given lubricant concentration, blending experiments, in which the mixing time was
87 greatly varied between 2 – 600 min, were executed, and the derived compactibility reduction was
88 modeled by adapting the dispersion model proposed by Schilde et al. [31].

89 **2. Methods and Materials**

90 **2.1 Particle size analysis**

91 Particle size distributions were measured by means of laser diffraction (MasterSizer 3000, Malvern
92 Panalytical, USA). Powders were dispersed by using the dry dispersion unit AERO S and applying a
93 dispersion pressure of 0.5 bar. Samples were measured in triplicate, and an average particle size

94 distribution was calculated. Additionally, the specific surface area $S_{m,LD}$ was calculated based on the
95 particle size distribution and considering the solids density ρ_s .

96 2.2 Solids density

97 Solids densities ρ_s were measured by means of helium pycnometry (Ultrapyc 1200e, Micromeritics,
98 USA). For each material, three samples were investigated in a ten-fold measurement and an average
99 solids density was calculated.

100 2.3 Scanning electron microscopy

101 Particle morphology was investigated by means of scanning electron microscopy (SEM; Helios G4 CX,
102 Thermo Fisher Scientific, USA). Samples were sputtered with gold (LEICA EM ACE600, Leica
103 microsystems GmbH, Germany).

104 2.4 Gas adsorption analysis

105 Specific surface areas of lubricants were analyzed by gas adsorption measurements (ASAP 2460,
106 micromeritics, USA) applying the 5-point BET method. Samples were conditioned under vacuum at
107 25 °C overnight. Nitrogen was used as an adsorptive. Powders were analyzed in triplicate and an average
108 specific surface area $S_{m,BET}$ was calculated.

109 2.5 Blending

110 Blends of 50 g were produced by means of a Turbula mixer (T2F, Willy A. Bachofen GmbH, Germany)
111 using 1 L glass bottles. For all blends, a rotation frequency of 49 min⁻¹ was applied. The effect of
112 lubricant concentration on the mechanical tablet strength was evaluated by systematically varying the
113 lubricant concentration between 0.25 and 2 wt.% and applying a mixing time of 2 min. In order to
114 examine the effect of mixing time on mechanical strength, binary blends of MCC and MgSt were
115 produced with a fixed lubricant concentration of 0.5 wt.% for varying mixing times (2 – 600 min).
116 Additionally, binary blends of MCC and MgSt with very small to medium amounts of MgSt (0.02 – 1
117 wt.%) were produced by applying a mixing time of 120 min.

118 2.6 Compaction

119 Tablets were produced by a compaction simulator (Stylone evolution, Medelpharm, France), which was
120 equipped with 11.28 mm round, flat-faced tooling. In the case of formulations containing MCC_{fine} or
121 MCC_{medium}, dies were filled by hand after manually weighing the desired powder mass. For MCC_{coarse},
122 a gravity feeder was applied to fill the dies. Independently of the filling method, a tablet weight of
123 approximately 450 mg was used. The compression profile of a StylCam (Medelpharm, France) with a
124 rotation frequency of 5 min⁻¹ was simulated. The compression stress was systematically varied between
125 50 and 300 MPa. For each set of process parameters, five tablets were produced and stored under lab
126 conditions (20 ± 1 °C, 40 ± 10% r.H.).

127 2.7 Tablet analysis

128 After measuring the tablet weight m_t , the tablet height h_t and tablet diameter d_t were determined by a
129 tablet tester (MultiTest 50 FT, Dr. Schleuniger, Switzerland). By relating the resulting tablet density
130 ρ_{tablet} to the solids density ρ_s , the tablet porosity ε was calculated:

$$\varepsilon = 1 - \frac{\rho_{tablet}}{\rho_s} = 1 - \frac{4 \cdot m_t}{\pi \cdot d_t^2 \cdot h_t \cdot \rho_s} \quad (1)$$

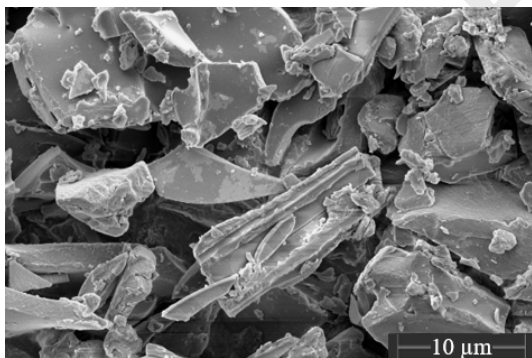
131 Afterwards, the tablet breaking force F_B was measured by a diametral compression test (MultiTest 50
132 FT, Dr. Schleuniger, Switzerland) with a loading rate of 0.35 mm s^{-1} . The resulting tablet tensile strength
133 σ_t was calculated according to the equation of Fell and Newton [32]:

$$\sigma_t = \frac{2 \cdot F_B}{\pi \cdot d_t \cdot h_t} \quad (2)$$

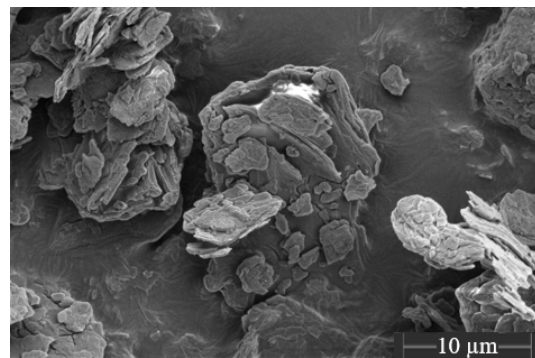
134 2.8 Materials

135 Three different grades of microcrystalline cellulose (Vivapur 101 (MCC_{fine}), Vivapur 102 ($\text{MCC}_{\text{medium}}$)
136 and Vivapur 200 ($\text{MCC}_{\text{coarse}}$), all JRS Pharma, Germany) were considered in this study. For lubrication,
137 four different grades of magnesium stearate (Carl Roth, Germany (MgSt_1); Faci, Italy (MgSt_3); Ligamed
138 MF-2-V, Peter Greven GmbH, Germany (MgSt_2); Ligamed MF-3-V, Peter Greven GmbH, Germany
139 (MgSt_4)) were used. Prior to application, lubricants were deagglomerated by using a $355 \mu\text{m}$ sieve.

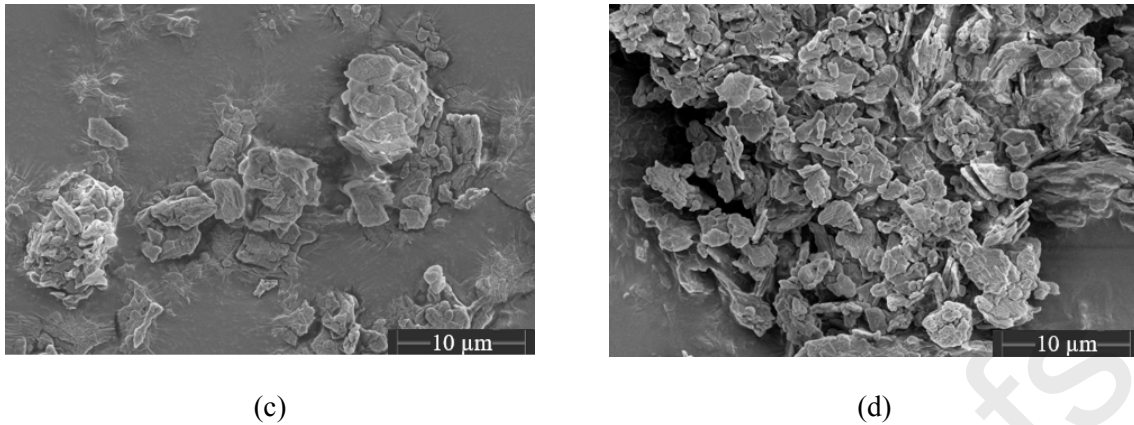
140 The morphology and particle size of the investigated lubricants were investigated by means of SEM
141 images. The nomination of MgSt grades follows their median particle size (cf. Figure 1 and Figure 2b).
142 MgSt_2 , MgSt_3 , and MgSt_4 exhibit a comparable particle morphology in which the platelet-shaped
143 primary particles are agglomerated into coarser secondary particles. It is generally believed that during
144 blending processes, acting shear stress results in the dispersion of these primary lubricant particles for
145 prolonged mixing times [5,33]. In contrast, MgSt_1 consists of considerably larger primary particles,
146 which showed a limited surface roughness to which smaller particles are attached. Generally, all
147 investigated MgSt grades exhibit a monomodal particle size distribution whereby the median particle
148 size ranges between $17.2 \mu\text{m}$ (MgSt_1) and $6.9 \mu\text{m}$ (MgSt_4) (Table 1 and Figure 2).



(a)

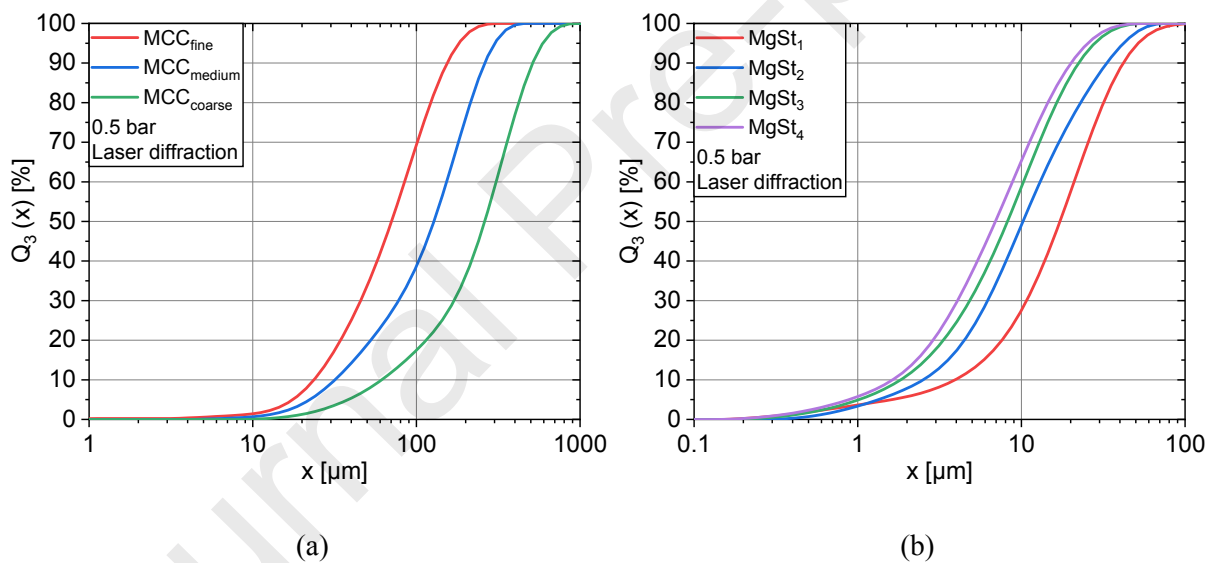


(b)



149 Figure 1: SEM images of MgSt₁ (a), MgSt₂ (b), MgSt₃ (c) and MgSt₄ (d)

150 The applied MCC grades possess considerably larger particles, as shown in Figure 2a. The cumulative
 151 particle size distributions revealed expected differences between the applied MCC grades, as the median
 152 particle sizes significantly differed between 70 μm (MCC_{fine}) and 261 μm (MCC_{coarse}) (Table 1).



153 Figure 2: Cumulative particle size volume distributions of the investigated grades of MCC (a) and MgSt
 154 (b) determined by laser diffraction for a dispersion pressure of 0.5 bar.

155 Additionally, the specific surface areas of the lubricants determined by gas adsorption substantially
 156 differ between 0.95 m² g⁻¹ (MgSt₁) and 34.45 m² g⁻¹ (MgSt₄) and do not follow the order of median
 157 particle size. This discrepancy can be attributed to the different primary particle size of the lubricant
 158 particles examined which determine the $S_{m,BET}$ values. Contrarily, the x_{50} values correspond to the
 159 secondary particle size of the visible lubricant agglomerates. Thus, the investigated lubricants show
 160 significant differences in their particulate structure, the influence of which on the dispersion behavior is
 161 investigated in this study.

162 Table 1: Bulk properties of investigated diluents and lubricants. Specific surface area values represent
 163 average values ± standard deviation.

Diluent	x_{50} [μm]	Lubricant	x_{50} [μm]	$S_{m,BET}$ [$\text{m}^2 \text{g}^{-1}$]
MCC _{fine}	70 ± 0.1	MgSt ₁	17.2 ± 0.07	0.95 ± 0.05
MCC _{medium}	128 ± 1.4	MgSt ₂	10.2 ± 0.03	14.14 ± 0.3
MCC _{coarse}	261 ± 9.9	MgSt ₃	8.2 ± 0.07	3.18 ± 0.09
		MgSt ₄	6.9 ± 0.33	34.45 ± 3.1

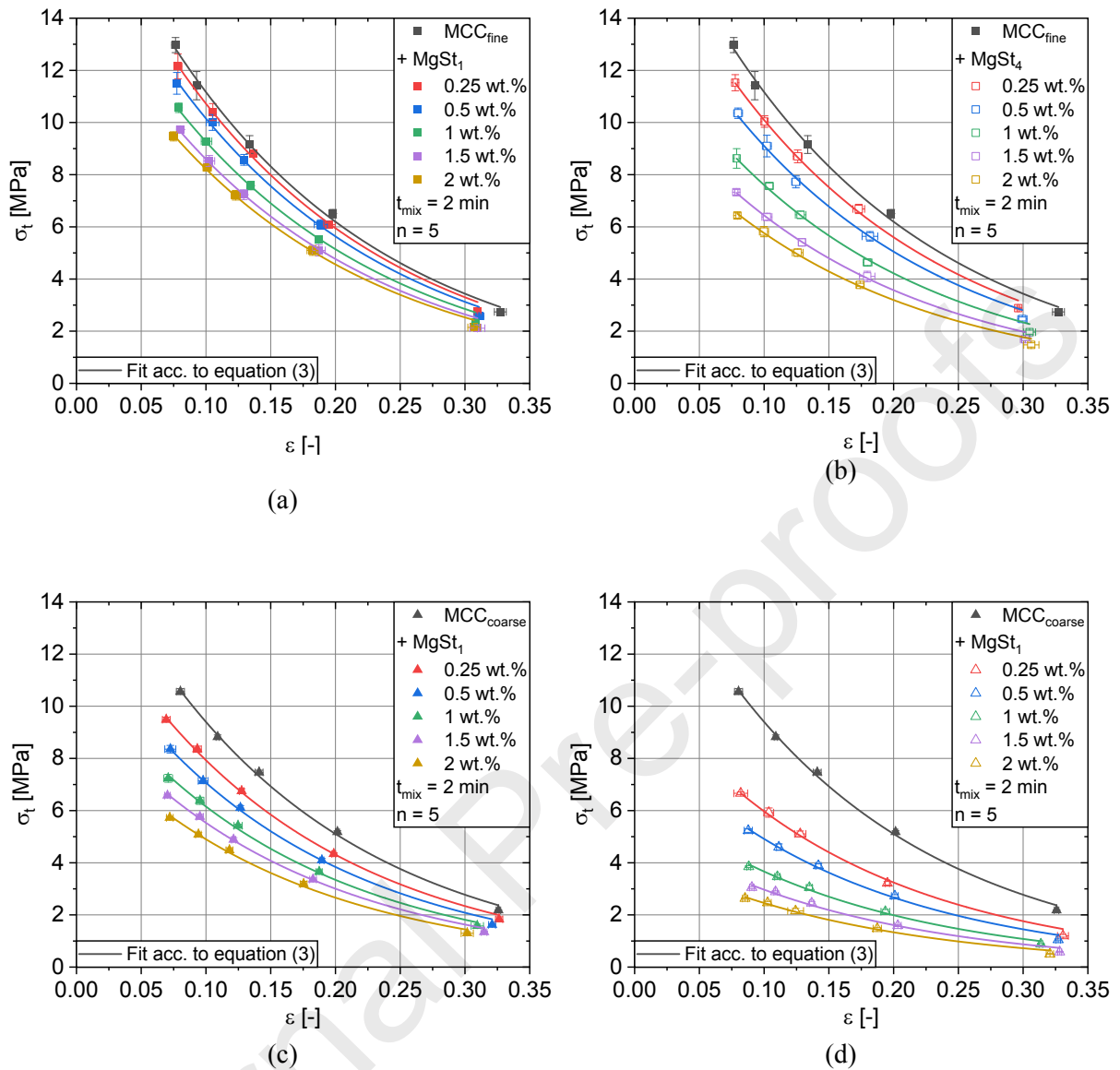
164 3. Results and Discussion

165 3.1 Impact of lubricant concentration on mechanical strength of tablets

166 In a first step, the impact of lubrication on the mechanical strength of MCC tablets was investigated by
 167 applying short mixing times of 2 min and systematically varying the MgSt concentration between 0.25
 168 and 2 wt.%. Here, the relationship between tablet porosity and tensile strength, the compactibility, was
 169 evaluated. The compactibility is only slightly impacted by changes in compaction kinetics [34] and thus,
 170 can be seen as a fundamental relationship that describes the bondability of the formulation. Rumpf's
 171 model suggests that the bondability of a compact depends on the quantity and strength of bonds formed
 172 on the aggregate [35] and can be calculated based on porosity, coordination number, particle surface
 173 area, and bonding force.

174 The internal lubricant addition results in the surface coverage of diluent particles by lubricant particles
 175 [5,6]. In the case of lubricated MCC, it can be hypothesized that the negative impact on mechanical
 176 strength can be explained by two different mechanisms [36]: First, the presence of lubricants on the
 177 surface acts as a physical barrier, preventing, amongst other adhesive forces, strong hydrogen bonding
 178 between MCC particles [37] and replacing them with weaker bonding between lubricant and MCC
 179 particles. Second, the decreased bonding force of lubricated MCC particles enhances the extent of
 180 relaxation during decompression [38] and by doing so, increases the interparticulate distance, reducing
 181 effective particle interaction areas.

182 In this study, MCC was applied as a model material, as its tensile strength is highly sensitive to the
 183 addition of lubricants [39], especially due to the limited generation of new, unlubricated surfaces during
 184 compaction [7,8]. Consequently, this high sensitivity enables the correlation of the dispersion behavior
 185 of MgSt with the process and formulation parameters used in this study. As expected, increasing the
 186 concentration of internally applied lubricants results in a severe decrease in the compactibility of binary
 187 formulations of MCC and MgSt (Figure 3).



188 Figure 3: Compactibility plots of binary formulations of MCC and MgSt for different lubricant
 189 concentrations and a mixing time of 2 min. Lines represent fits acc. to equation (3) with a fixed k_b value
 190 determined from the unlubricated MCC grades, named $k_{b,dil}$ (a) MCC_{fine} + MgSt₁ (b) MCC_{fine} + MgSt₄
 191 (c) MCC_{coarse} + MgSt₁ (d) MCC_{coarse} + MgSt₄

192 The compactibility of tablets was quantified by applying the equation of Ryshkewitch-Duckworth
 193 [40,41]:

$$\sigma_t = \sigma_0 \cdot e^{-k_b \cdot \epsilon} \quad (3)$$

194 Where σ_0 is the theoretical maximal tensile strength for a non-porous tablet and k_b is the bonding
 195 capacity.

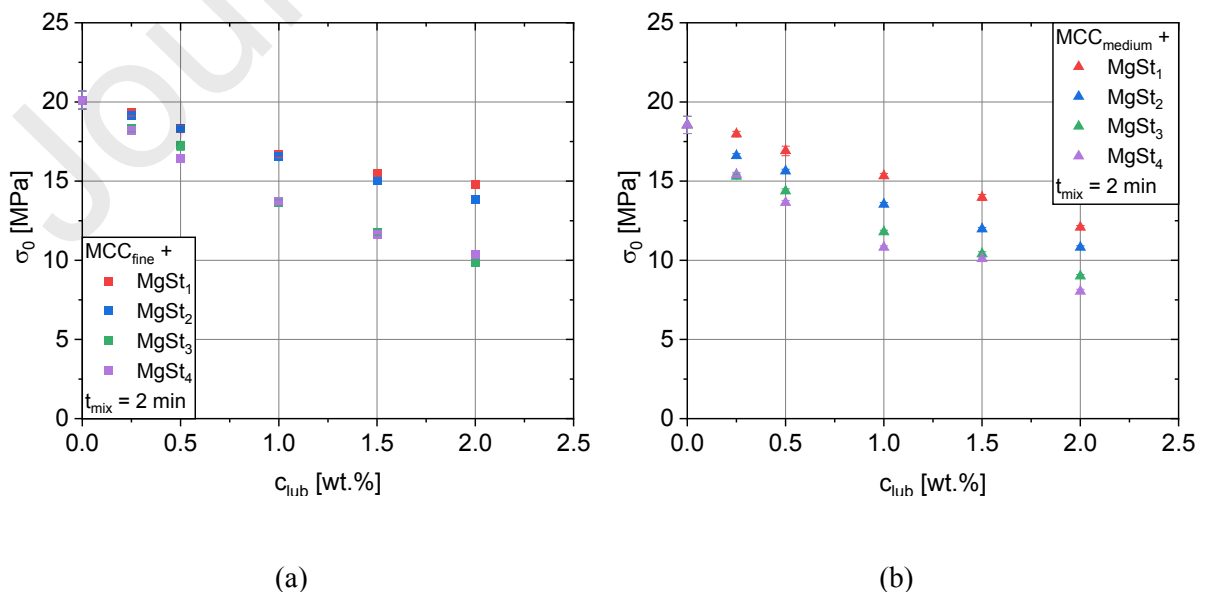
196 In a previous study of our research group, it was shown that the k_b values of lubricated MCC grades are
 197 virtually constant for different MgSt concentrations [28]. Thus, in order to limit the effect of lubrication
 198 to the reduction of σ_0 , the compactibility profiles of lubricated MCC formulations are fitted by the

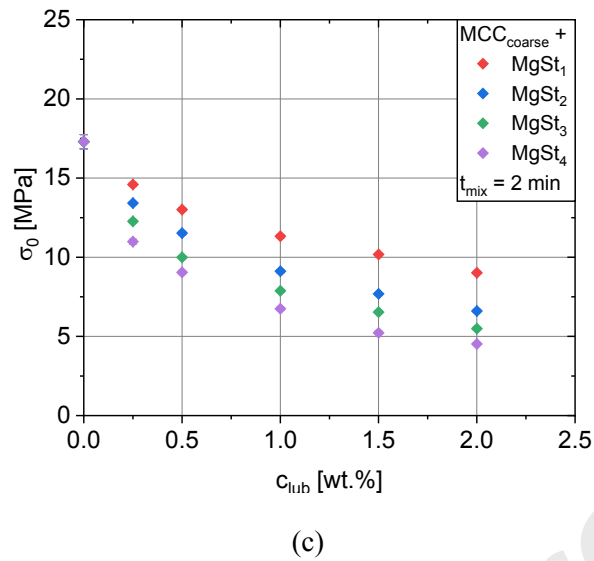
199 Ryshkewitch-Duckworth equation while using the k_b values of the unlubricated diluents $k_{b,dil}$,
 200 respectively. The empirical fit parameters of the unlubricated MCC grades were determined beforehand
 201 based on their compactibility profiles (Figure S1) and are enlisted in Table 2.

202 Table 2: Determined parameters of the Ryshkewitch-Duckworth equation for unlubricated MCC grades

Diluent	Bonding capacity k_b	
	Theoretical max. tensile strength σ_0 [MPa]	
	[-]	
MCC _{fine}	5.89 ± 0.24	20.12 ± 0.57
MCC _{medium}	5.9 ± 0.23	18.55 ± 0.54
MCC _{coarse}	6.1 ± 0.21	17.3 ± 0.45

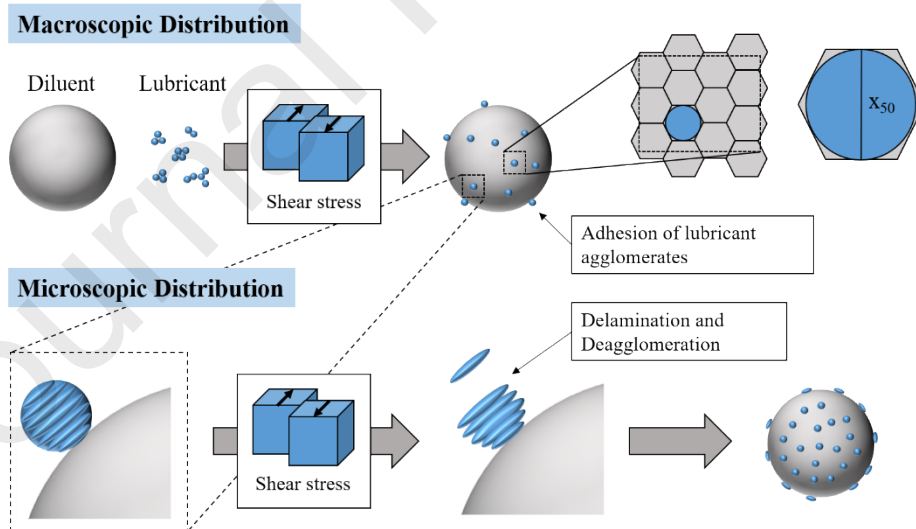
203 As expected and already shown in a previous publication [28], the subsequently derived theoretical
 204 maximal tensile strength values decrease for rising lubricant concentrations (Figure 4). Obviously, if
 205 finer MgSt grades (e.g., MgSt₄) are applied, smaller σ_0 values result for a given lubricant concentration.
 206 This detrimental effect of smaller lubricant particles on the mechanical tablet strength is well known
 207 [21,42] and can be explained by the higher number of lubricant particles for a given lubricant
 208 concentration, resulting in a higher coverage of diluent particles. Consequently, a greater fraction of
 209 comparably stronger MCC-MCC bonds is replaced by weak MCC-MgSt or MgSt-MgSt bonds and by
 210 that, the tablet strength decreases. Additionally, for a given lubricant grade and concentration, the
 211 application of coarser MCC particles results in a considerably higher reduction of compactibility (cf.
 212 Figure 4a and Figure 4c). This effect is caused by the smaller available diluent surface, which, if the
 213 same number of lubricant particles are applied, will be covered to a greater extent by lubricant particles.
 214 It is obvious that the extent of compactibility reduction depends on both applied diluent and lubricant
 215 particle size for binary formulations of MCC and MgSt, due to the different resulting surface coverages.
 216 In previously conducted studies [21,42], the same qualitative explanatory approach was used, but no
 217 quantitative correlation taking into account the particle sizes of both excipients was derived.





218 Figure 4: Correlation of lubricant concentration and theoretical max. tensile strength σ_0 for binary
 219 mixtures of MCC_{fine} (a), MCC_{medium} (b), MCC_{coarse} (c) and four different grades of MgSt for a mixing
 220 time of 2 min.

221 Measuring the extent of surface coverage by lubricant particles is experimentally challenging and time-
 222 consuming. As discussed above, quantitative values of surface coverage by MgSt are typically based on
 223 SEM measurements. However, identifying MgSt on MCC particles is extremely challenging as the
 224 debris of MCC and MgSt exhibit comparable morphologies [5] and MCC particles do not exhibit the
 225 required smooth particles surfaces [15].



226

227 Figure 5: Schematic representation of the proposed dispersion mechanisms during mixing of MgSt and
 228 diluent particles. Initially, lubricant agglomerates adhere to the diluent surface and occupy a hexagonal
 229 shaped area according to their x_{50} . If further shear stress is applied, MgSt particles deagglomerate or
 230 delaminate into platelets, which consecutively cover additional diluent surfaces.

231 In the course of this study, the dispersion mechanisms proposed by Shah and Mlodozieniec are
 232 considered [5]. The dispersion of MgSt due to shear stress can thereby be distinguished in two
 233 consecutive steps: First MgSt stearate agglomerates adhere to the diluent surfaces resulting in a
 234 macroscopic distribution of the lubricant. If further shear stress is applied, the lubricant agglomerates

235 deagglomerate or delaminate, due to their lamellar structure, into smaller particles and which
 236 consecutively cover additional diluent surfaces (Figure 5).

237 The resulting macroscopic lubricant distribution was theoretically estimated by calculation of the
 238 geometric surface coverage according to the approach of Meyer [43]. It is assumed that each lubricant
 239 particle occupies a hexagonal area on the diluent surface according to its median particle size x_{50} (Figure
 240 5). For this methodology, several assumptions are drawn:

- 241 1. For short mixing times, the lubricant agglomerates are distributed on the diluent surfaces due to
 242 acting shear stresses and occupies the diluent surface. No further deagglomeration or
 243 delamination has taken place.
- 244 2. The different lubricant particle sizes after the macroscopic distribution can be represented by a
 245 characteristic particle size (x_{50}), which can reliably be measured by laser diffraction.
- 246 3. The available diluent surface can be estimated by the specific surface area calculated from
 247 particle size distributions measured by laser diffraction.
- 248 4. The deposition of lubricant agglomerates on free diluent surfaces is favored in terms of the
 249 formation of lubricant multilayer on the diluent surface

250 Naturally, those assumptions do not represent the distributed nature of particle properties of both
 251 diluents and lubricants as well as the irregular shape of those entities. However, in a previous
 252 publication, this approach was successfully applied to link the effect of lubrication to the prediction of
 253 multi-component mixtures [30] and to identify a common relationship between compactibility reduction
 254 and lubricant particles size of chemically different lubricants [19].

255 The total available diluent surface S_{dil} can be calculated by multiplying the specific surface area $S_{m,LD}$
 256 with the total diluent mass m_{dil} :

$$S_{dil} = S_{m,LD} \cdot m_{dil} \quad (4)$$

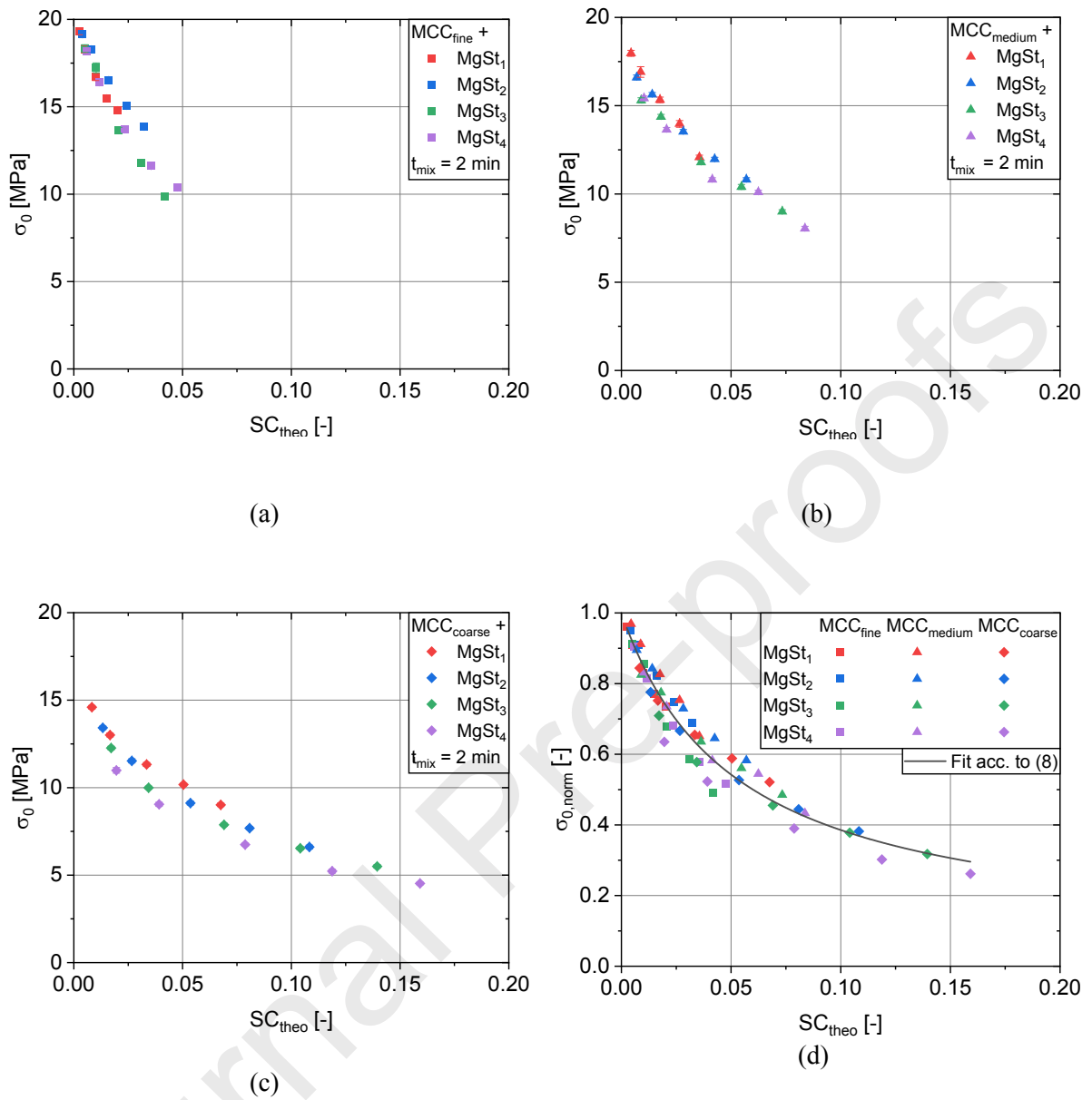
257 The occupied area by lubricant particles S_{lub} can be derived by [43]:

$$S_{lub} = n_{lub} \cdot S_{lub,particle} = \left(\frac{m_{lub}}{\frac{\pi}{6} \cdot x_{50,lub}^3 \cdot \rho_{s,lub}} \right) \cdot \frac{\sqrt{3}}{2} \cdot x_{50,lub}^2 \quad (5)$$

258 Where $x_{50,lub}$ is the median particle size of the investigated lubricant and m_{lub} is the total lubricant mass.
 259 Afterwards, the particle size-based theoretical surface coverage SC_{theo} can be calculated:

$$SC_{theo} = \frac{S_{lub}}{S_{dil}} \quad (6)$$

260 By relating SC_{theo} to σ_0 values of lubricated blends, a unifying relationship for binary blends of a given
 261 MCC grade and different MgSt grades was identified (Figure 6a-c). For all applied MCC grades, an
 262 exponential decrease of σ_0 for rising SC_{theo} values was observed.



263 Figure 6: Correlation between σ_0 and SC_{theo} for binary blends of MCC_{fine} (a), MCC_{medium} (b), MCC_{coarse}
 264 (c) and four different grades of MgSt. Correlation between $\sigma_{0,norm}$ and SC_{theo} for all investigated blends
 265 of three different MCC and four different MgSt grades (d).

266 In case of unlubricated MCC tablets, despite being generally comparable, a slight trend of higher σ_0
 267 values for finer MCC grades was determined (Table 2). This difference in initial compactibility impedes
 268 the direct comparison of σ_0 values of lubricated MCC grades. In order to allow a meaningful comparison
 269 of different grades, the derived $\sigma_{0,lub}$ values of lubricated formulations were normalized by the $\sigma_{0,dil}$
 270 values of the unlubricated MCC grade, respectively:

$$\sigma_{0,norm} = \frac{\sigma_{0,lub}}{\sigma_{0,dil}} \quad (7)$$

271 Plotting $\sigma_{0,norm}$ against SC_{theo} reveals a unifying compactibility reduction for higher SC_{theo} values. This
 272 finding indicates that the initial MgSt dispersion is governed by the macroscopic distribution of lubricant
 273 agglomerates, as previously assumed [5], and depends on the initial particle sizes of applied excipients.
 274 The reduction of $\sigma_{0,norm}$ was modeled by fitting the data with an appropriate dispersion kinetic. Here, the
 275 dispersion kinetic published by Schilde et al. was adapted [31], which depicts a modified Michaelis-
 276 Menten kinetic:

$$\sigma_0 = \sigma_{0,dil} + (\sigma_{0,end} - \sigma_{0,dil}) \cdot \frac{SC_{theo}}{SC_{theo} + K_{Macro}} \quad (8)$$

277 Where $\sigma_{0,end}$ describes the minimal σ_0 value and K_{Macro} represents an empirical kinetic constant. By
 278 considering equation (7), equation (9) can be yielded:

$$\sigma_{0,norm} = 1 + (\sigma_{0,end,norm} - 1) \cdot \frac{SC_{theo}}{SC_{theo} + K_{Macro}} \quad (9)$$

279 Generally, it can be hypothesized that the minimal value of $\sigma_{0,norm}$ should be close to zero due to the
 280 weak interactions between MgSt particles, however, results shown in later chapters indicate that the
 281 threshold value will most likely be different to zero. Additionally, it is questionable if the threshold can
 282 be reasonably assessed, as a further increase of SC_{theo} resulted in obvious tablet defects. As the
 283 investigated lubricant concentrations are well within the industrially applied range, higher lubricant
 284 concentrations were not examined.

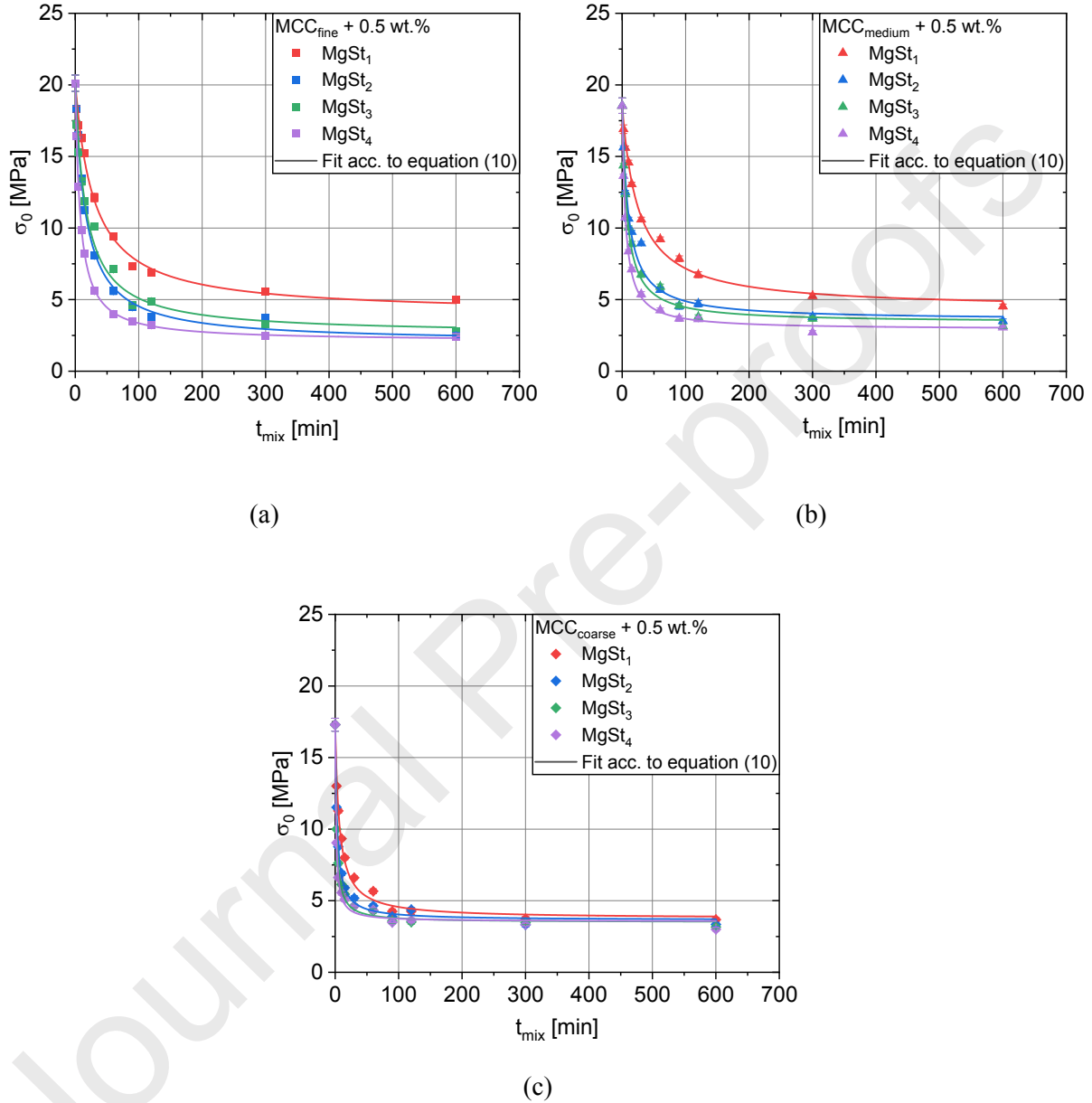
285 Generally, alternative dispersion models [4,23] were also evaluated, but resulted in poorer correlation
 286 (data not shown). As shown in Figure 6d, the adapted dispersion kinetic accurately describes the plotted
 287 data ($R^2 \sim 0.95$) and thereby, once parametrized by a limited number of experiments, can be used to
 288 predict the compactibility loss due to lubrication of MCC for different excipient particle sizes. However,
 289 as 12 individual combinations of materials are taken into account, a maximum deviation of approx. 15%
 290 of single values from the model occurs. Consequently, the proposed approach represents an interesting
 291 tool for formulation development, as it requires only comparatively easily measurable particle properties
 292 and allows the adaptation to partially unavoidable changes in the starting material quality.

293 3.2 Impact of mixing time on mechanical strength of tablets

294 The interplay of MgSt and MCC particle sizes on the dispersion behavior of MgSt for prolonged mixing
 295 times was evaluated by creating binary formulations with a fixed MgSt concentration of 0.5 wt.% and
 296 systematically varying the mixing time between 2 and 600 min. For longer mixing times, it is proposed
 297 that MgSt deagglomerates and delaminates resulting in an increased coverage of MCC surfaces (Figure
 298 5). Accordingly, with increased mixing time, the compactibility is reduced (Figure S2) and can be
 299 quantified by applying the Ryshkewitch-Duckworth equation (3). Analogous to the impact of lubricant
 300 concentration, the $k_{b,dil}$ value of the unlubricated MCC grades was used to limit the effect of lubricant
 301 addition to σ_0 . Subsequently, the σ_0 vs. t_{mix} plots were evaluated by applying the adapted dispersion
 302 kinetic of Schilde et al. [31]:

$$\sigma_0 = \sigma_{0,dil} - (\sigma_{0,dil} - \sigma_{0,end}) \cdot \frac{t_{mix}}{t_{mix} + K_{Micro}} \quad (10)$$

303 Where K_{Micro} is a kinetic constant describing the half life time until 50% of the absolute difference
 304 between $\sigma_{0,dil}$ and $\sigma_{0,end}$ is reached. The compactibility for a mixing time of 0 min was estimated by
 305 applying the σ_0 value of the unlubricated diluent $\sigma_{0,dil}$. The $\sigma_{0,dil}$ values have been quantified beforehand
 306 (Table 2), leaving only $\sigma_{0,end}$ and K_{Micro} to be determined.



307 Figure 7: Effect of mixing time t_{mix} on σ_0 values of binary blends of MCC_{fine} (a), MCC_{medium} (b), MCC_{coarse}
 308 (c) and different grades of MgSt for a lubricant concentration of 0.5 wt.%. The σ_0 value for a mixing
 309 time of 0 min was estimated by $\sigma_{0,dil}$.

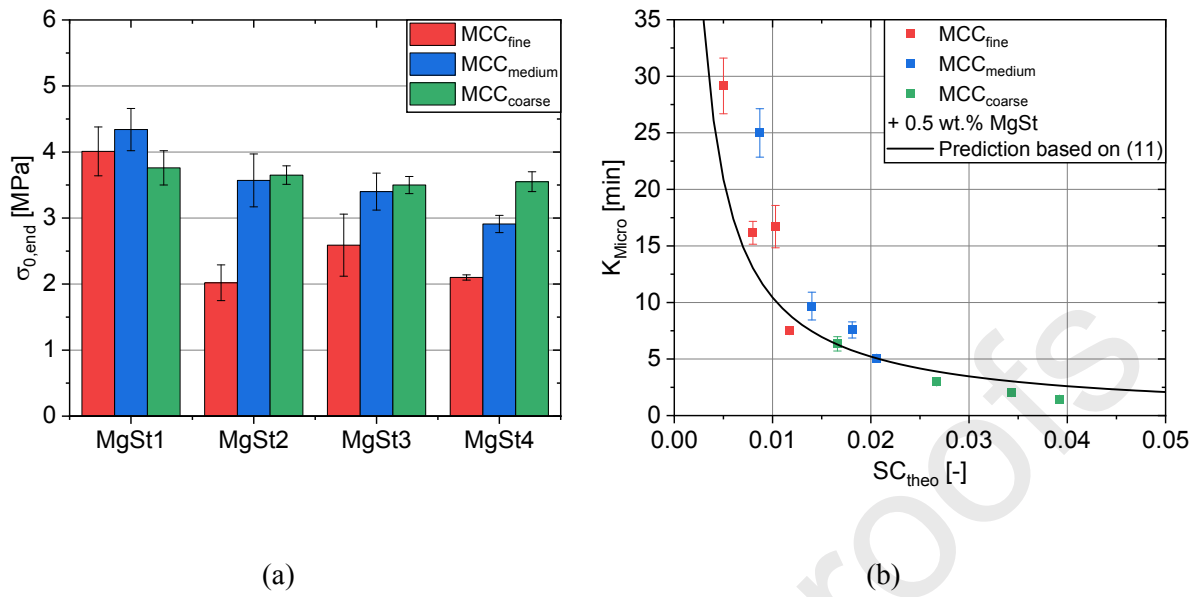
310 As shown in Figure 7, the determined σ_0 values decrease with rising mixing time whereby two phases
 311 can be identified: A drastic reduction rate for short mixing times followed by a considerably smaller
 312 reduction rate for long mixing times. This reduction rate represents the lubricant dispersion rate.
 313 Generally, the majority of investigated formulations approach a common threshold ($\sigma_{0,end}$) between 2.5
 314 – 4 MPa for all investigated formulations. Contrary to this finding, if MgSt₁ in combination with MCC_{fine}
 315 or MCC_{medium} is applied, the minimum σ_0 value is slightly higher. Those visible differences are not
 316 completely resembled by the $\sigma_{0,end}$ values due to the extrapolating nature of the applied fit function
 317 (Figure 8a).

318 The minimal compactibility for long mixing times can be interpreted as an equilibrium state of lubricant
319 dispersion. Assuming that the mixing time of 600 min excludes a limitation due to an insufficient
320 number of stress events, three different scenarios can be envisioned (amongst others) to explain this
321 equilibrium state:

- 322 1) The shear stress is insufficient to induce further MgSt delamination due to an increase of shear
323 strength with decreasing particle size of MgSt during mixing. The equilibrium state reflects the
324 maximum surface coverage depending on the lubricant shear strength, lubricant mass and
325 available diluent surface.
- 326 2) The shear stress exceeds the shear strength of MgSt at any given time during mixing, resulting
327 in a complete dispersion of the applied MgSt mass. The resulting number and size of MgSt
328 particles is insufficient to cover the available MCC surface. The equilibrium state is defined by
329 the lubricant mass and available MCC surface.
- 330 3) The shear stress is sufficiently high to disperse MgSt into particles, which size and number is
331 sufficient to cover the available MCC surface. The equilibrium state is defined by the remaining
332 bonding potential of lubricated MCC surfaces.

333 Based on the results shown, the deviating results for $MgSt_1 + MCC_{fine}/MCC_{medium}$ could be explained by
334 scenario 1, indicating an increased shear strength of the applied $MgSt_1$ compared to the other grades.
335 This hypothesis is supported by the fact that $MgSt_1$ is a technical grade of MgSt in contrast to $MgSt_2 -$
336 $MgSt_4$ that resemble pharmaceutical grades. Technical grades with a higher stearate content are known
337 to exhibit higher shear strength [44]. If the coarsest MCC grade with a decreased total surface is applied,
338 the resulting particle size and number of particles after delamination of $MgSt_1$ is sufficient to cover the
339 available MCC surface, similar to the other MgSt grades (Figure 7c).

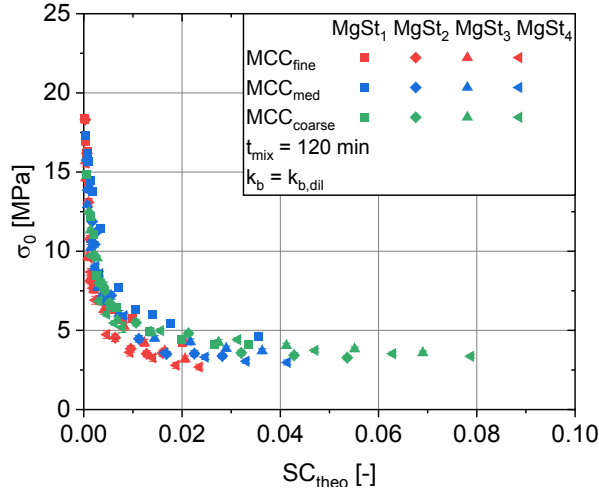
340 If Scenario 2 would be valid, for a given lubricant mass the total surface to be covered determines the
341 fraction of surface coverage and by that, the minimal compactibility. As the total surface to be covered
342 is determined by the MCC grade, coarser MCC grades should generally exhibit smaller compactibility
343 values. In fact, a slight tendency for an opposing effect is apparent: coarser MCC grades show slightly
344 higher $\sigma_{0,end}$ values (Figure 8a). It could be hypothesized that larger MCC particles exhibit a greater
345 absolute deformation during compaction, which could result in an increased interference with the
346 lubricant coverage. Additionally, a small degree of fragmentation was identified for coarse MCC grades
347 by Roberts and Rowe [45]. Both mechanisms could result in an increase of fresh, unlubricated surfaces
348 that are available for bonding, which could explain the slightly higher $\sigma_{0,end}$ values of coarser MCC
349 grades. However, though it may prevail during the whole dispersion process, this specific effect can
350 only be differentiated towards $\sigma_{0,end}$ because at lower dispersion states, the higher surface coverages of
351 coarser MCC particles overrule this effect by lower strength compared with smaller MCC particles. This
352 finding in combination with the general similarity of the found $\sigma_{0,end}$ values contradicts scenario 2.



353 Figure 8: Derived $\sigma_{0,end}$ (a) and K_{Micro} (b) values by fitting σ_0 vs. t_{mix} plots with equation (10) for different
 354 binary combinations of MCC and MgSt grades. Line in (b) represents prediction of K_{Micro} based on
 355 equation (11) and K_{Macro} derived of Figure 6d.

356 Thus, it can be hypothesized that scenario 3 best describes the equilibrium state for the majority of
 357 investigated formulations. To check this hypothesis, it was investigated whether the identified common
 358 equilibrium state is the consequence of the constant added lubricant mass or refers to the saturation of
 359 the majority of available MCC surfaces. Therefore, binary mixtures of all MCC grades and MgSt grades
 360 were created by applying a mixing time of 120 min and systematically varying the lubricant
 361 concentration between 0.02 – 1 wt.% (for MgSt₁ also 2 wt.%) (Figure S3). The mixing time of 120 min
 362 was chosen in order to ensure a sufficiently high number of stress events to achieve higher dispersion
 363 and to come close to a possible equilibrium while simultaneously keeping the experiments feasible in
 364 terms of time.

365 Afterwards, the compactibility profiles were mathematically quantified by applying the Ryshkewitch-
 366 Duckworth equation while assuming that the bonding capacity can be estimated by the bonding capacity
 367 of the unlubricated diluent $k_{b,dil}$. The resulting σ_0 values are plotted against the SC_{theo} , which represents
 368 the surface coverage of MCC after the macroscopic lubricant dispersion. It is evident, that a common
 369 relationship between σ_0 and SC_{theo} irrespective of the applied formulation can be identified (Figure 9).



370

371 Figure 9: Reduction of σ_0 as a function of SC_{theo} for different binary mixtures of MCC and MgSt for a
 372 mixing time of 120 min.

373 The resulting σ_0 values rapidly decrease between initial SC_{theo} values of 0 – 0.01 and subsequently
 374 approach a threshold of σ_0 between 3 – 4 MPa, similar to the results shown in Figure 7. Thereby, if a
 375 sufficient amount of lubricant is added to the formulation, a similar equilibrium state of compactibility
 376 results. This indicates that this equilibrium describes the residual bonding potential of lubricated MCC
 377 surfaces. Interestingly, higher MgSt₁ concentrations also results in a comparable minimum σ_0 values.
 378 This can be seen as confirmation that the deviating results for MgSt₁ + MCC_{fine}/MCC_{medium} is in fact
 379 attributed to its enhanced shear strength and does not indicate an entirely different behavior. Generally,
 380 the dataset can be divided into a rapid decrease of σ_0 followed by a very slow decrease of σ_0 . The
 381 transition area is located at SC_{theo} values of 0.01, which can be seen as a minimum value to ensure a
 382 common equilibrium state for high mixing times. This correlates to lubricant concentrations between
 383 0.1 wt.% (MCC_{coarse} + MgSt₄) and 1 wt.% (MCC_{fine} + MgSt₁) and is well within the commonly applied
 384 range of pharmaceutical lubricant concentrations. Thus, from a practical point of view, a common
 385 minimal compactibility value can be assumed. For SC_{theo} values below 0.01, considerably higher σ_0
 386 values were found. This increased compactibility could either be caused by an insufficient lubricant
 387 mass or an insufficient number of stress events. As those small lubricant concentrations are typically not
 388 applied, no further laborious experiments with prolonged mixing times were performed.

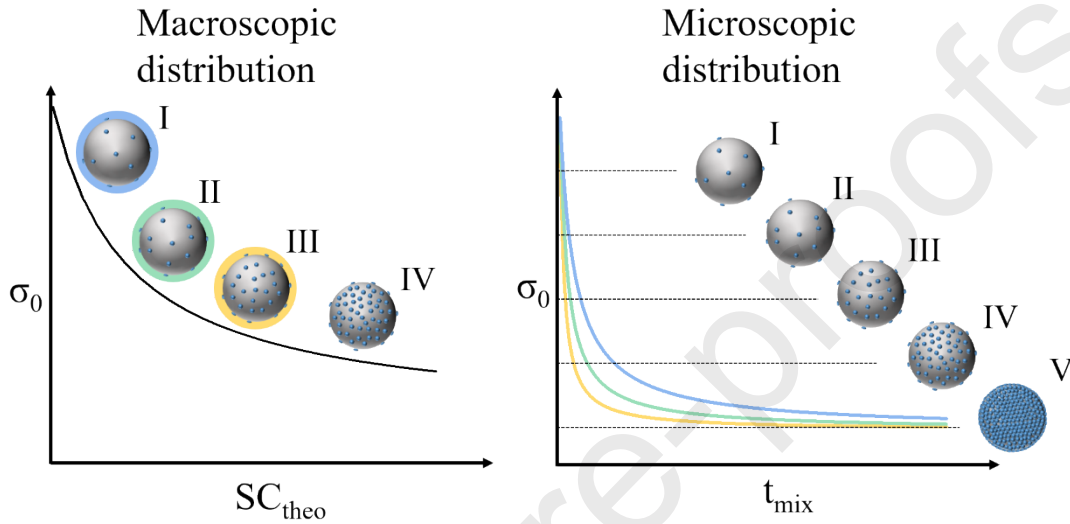
389 Thereby, following the stress model for comminution processes by Kwade [46], it can be hypothesized
 390 that the complete saturation of available MCC surfaces by MgSt particles can be achieved if the
 391 following criteria are met:

- 392 1. During mixing, the stress energy during stress events is sufficiently high to enable the
 393 lubrication dispersion, i.e. by deagglomeration and delamination.
- 394 2. The applied mixing time is sufficiently long in order to ensure a sufficient number of successful
 395 stress events, which result in lubricant delamination.
- 396 3. The applied lubricant mass is sufficiently high, so that the number and size of generated
 397 lubricant particles after delamination is sufficient to cover the available MCC surfaces.

398 Assuming that the $\sigma_{0,dil}$ values are known and $\sigma_{0,end}$ values can be reasonably estimated, the dispersion
 399 behavior is mainly governed by the dispersion rate. The dispersion rate describes the rate of which a
 400 given MCC surface is covered by lubricant particles and is quantified by the kinetic constant, K_{Micro} .
 401 Here, K_{Micro} represent the necessary mixing time until σ_0 is reduced by 50% of the difference between
 402 $\sigma_{0,dil}$ and $\sigma_{0,end}$. Thus, smaller K_{Micro} values represent a fast dispersion rate and vice versa.

403 Correlating the kinetic constant K_{Micro} to SC_{theo} , which represents the macroscopic lubricant dispersion,
 404 reveals a rapid decrease of K_{Micro} for increasing SC_{theo} values (Figure 8b). This relationship can be
 405 mechanistically understood as the probability that an individual available MCC surface spot is covered

406 by MgSt in a given time step. It is envisioned, that the delamination of lubricant particles due to shear
 407 stresses acting during mixing occurs if a lubricant particle is stressed between two MCC particles, which
 408 effectively act comparable to grinding media [46]. If a higher degree of MCC surface is already covered
 409 by lubricant particles after the macroscopic lubricant dispersion, the probability to stress a lubricant
 410 particle during a stress event is increased. Thereby, the dispersion rate during MgSt delamination
 411 directly depends on the macroscopic dispersion state. It is assumed that the different consecutive realized
 412 dispersion states of the investigated formulations are comparable, irrespective of the applied particle
 413 sizes (Figure 10). Thus, higher SC_{theo} values can be understood as a headstart, which results in short
 414 necessary mixing times, and by that smaller K_{Micro} values, to completely cover the diluent surface.



415

416 Figure 10: Schematic representation of proposed dispersion states of MgSt as a function of the
 417 macroscopic and microscopic lubricant distribution.

418 Additionally, it can be assumed that the minimal compactibility of lubricated MCC is comparable
 419 independent of the type of distribution (be it macroscopic or microscopic) if sufficient amounts of
 420 lubricant are applied. Following, $\sigma_{0,dil}$ and $\sigma_{0,end}$ can be estimated to be equal. Assuming that the
 421 dispersion kinetics for the influence of concentration and mixing time coincide for a mixing time of
 422 2 min, the dependence of K_{Micro} on SC_{theo} can be determined analytically. Therefore, equation (8) and
 423 (10) are equated for $t_{mix} = 2$ min and solved for K_{Micro} :

$$K_{Micro} = \frac{2 \text{ min} \cdot K_{Macro}}{SC_{theo}} \quad (11)$$

424 Plotting the resulting predicted K_{Micro} values (Figure 8b) showed a correct trend between the predicted
 425 and experimental K_{Micro} values. This finding is valuable as it allows the prediction of the dispersion
 426 behavior for prolonged mixing times without performing any mixing experiments for prolonged times.
 427 Instead, once the impact of lubricant addition on tablet compactibility for a small number of lubricant
 428 concentrations is established (c.f. Figure 6d) and modeled by equation (8), the dispersion behavior can
 429 already be reasonable predicted.

430 In summary, the influence of particle size on delamination behavior of MgSt on MCC particles can be
 431 divided into two aspects. The minimal compactibility for long mixing times appears to be comparable
 432 for the vast majority of investigated formulations with a given MgSt concentration, indicating that this
 433 equilibrium state is controlled by the residual bonding strength between lubricated MCC surfaces. The
 434 kinetics of dispersion, on the other hand, depend significantly on the set particle size-based surface

435 coverage due to the macroscopic distribution of MgSt after short mixing times, as it directly affects the
 436 probability that a MgSt particle is stressed during MCC particle contact. The findings shown here allow
 437 to quantitatively model the particle size influence on the tablet strength of binary mixtures of MCC and
 438 MgSt for prolonged mixing times for the first time and by that, can provide a substantial improvement
 439 of the available formulation knowledge.

440 In future studies, it would be desirable to quantify the lubricant particle strength and relating it to stress
 441 conditions during relevant pharmaceutical unit operations, e.g. mixing, to further rationalize the
 442 lubricant selection. Additionally, as these study has focused on a given set of process parameters, it
 443 would be desirable to combine this approach with models which take into account the effect of mixing
 444 process parameters on the tablet strength, e.g. the model of Kushner [4]. Finally, an extension of the
 445 findings on multi-component mixtures would represent a considerable economic benefit, as it would
 446 allow minimizing the number of required experiments.

447 4. Conclusions

448 In this study, the influence of the excipient particle size on the compactibility of binary mixtures of
 449 MCC and MgSt was investigated using three grades of MCC and four grades of MgSt. The impact of
 450 formulation was quantified by estimating the theoretical surface coverage and subsequently, correlated
 451 with the reduction of compactibility. Here, the effect of lubricant concentration and mixing time on this
 452 correlation was investigated in detail.

453 It was shown that the compactibility reduction for short mixing times could be modeled independent of
 454 the grades used by introducing theoretical surface coverage, which describes the surface coverage of
 455 diluents surfaces after the macroscopic lubricant distribution for short mixing times. The theoretical
 456 surface coverage requires only easily measurable formulation properties and allows predicting the
 457 compactibility reduction if components are replaced by other grades with different particle sizes. In
 458 addition, it was shown that, for a sufficient lubricant amount, the minimum compactibility for long
 459 mixing times is comparable for the majority of the formulations investigated, if a industrially common
 460 low threshold (< 0.5 wt.%) is overcome. This allows to mathematically limit the influence of the
 461 lubricant addition on the compactibility for prolonged mixing times to the dispersion rate. It could be
 462 shown that this dispersion rate mainly depends on the given theoretical surface coverage, since it
 463 determines the probability that a lubricant particle is stressed during an MCC particle contact and, by
 464 that, the probability of successful lubricant dispersion events.

465 Accordingly, the relationships shown in this framework represent a significant improvement in
 466 formulation knowledge regarding the linkage of applied excipient sizes on the compactibility reduction
 467 of lubricated MCC tablets. This knowledge can be transferred to other formulation components and can
 468 be used to streamline the development of new tablet formulations, minimizing the necessary empirical
 469 testing. This approach can also be applied directly for granules, which are quite frequently used for
 470 tableting. It could even be extended to materials causing too high ejection stresses and tablet defects for
 471 the unlubricated case, when external lubrication is applied to assess their compactibility data.

472

473 Table of Symbols

d_t	tablet diameter
ε	the tablet porosity
F_B	tablet breaking force

h_t	tablet height
k_b	bonding capacity
K_{Macro}	empirical kinetic constant for macroscopic distribution of lubricant particles
K_{Micro}	empirical kinetic constant for microscopic distribution of lubricant particles
m_t	tablet mass
m_{dil}	total diluent mass
m_{lub}	total lubricant mass
ρ_{tablet}	tablet density
ρ_s	solids density
$S_{m,LD}$	specific surface area determined by laser diffraction
$S_{m,BET}$	specific surface area determined by gas adsorption
S_{dil}	total available diluent surface
S_{lub}	total area occupied by lubricant particles
SC_{theo}	particle size-based theoretical surface coverage
σ_t	tablet tensile strength
σ_0	theoretical maximal tensile strength for a non-porous tablet
$\sigma_{0,lub}$	σ_0 of lubricated formulations
$\sigma_{0,dil}$	σ_0 of pure diluents
$\sigma_{0,norm}$	$\sigma_{0,lub}$ normalized to $\sigma_{0,dil}$

$\sigma_{0,end}$	asymptotic value of σ_0 for high blending times
$\sigma_{0,end,norm}$	$\sigma_{0,end}$ normalized to $\sigma_{0,dil}$
t_{mix}	blending time
$x_{50,lub}$	median particle size of the lubricant

474

475

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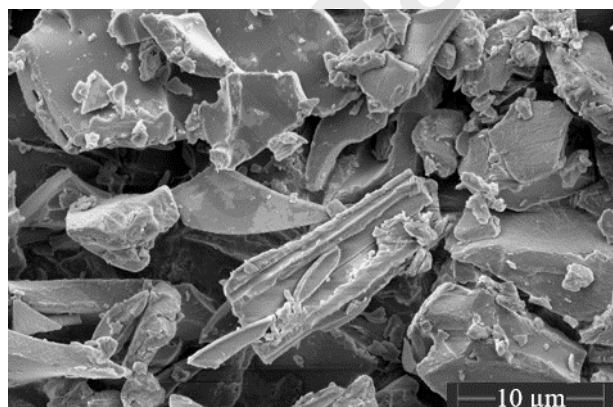
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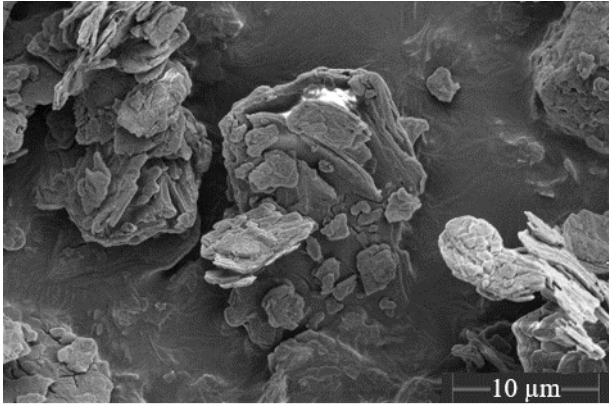
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- 598 **Daniel Puckhaber:** Conceptualization, Methodology, Validation, Formal analysis, Investigation,
599 Writing – Original Draft, Writing – Review & Editing, Visualization
- 600 **Jan Henrik Finke:** Conceptualization, Methodology, Validation, Formal analysis, Investigation,
601 Writing – Review & Editing, Visualization
- 602 **Sarah David:** Investigation, Writing – Review & Editing
- 603 **Bindhumadhavan Gururajan:** Investigation, Writing – Review & Editing
- 604 **Supriya Rane:** Project administration, Resources
- 605 **Arno Kwade:** Conceptualization, Investigation, Resources, Writing – Review & Editing, Supervision,
606 Project administration

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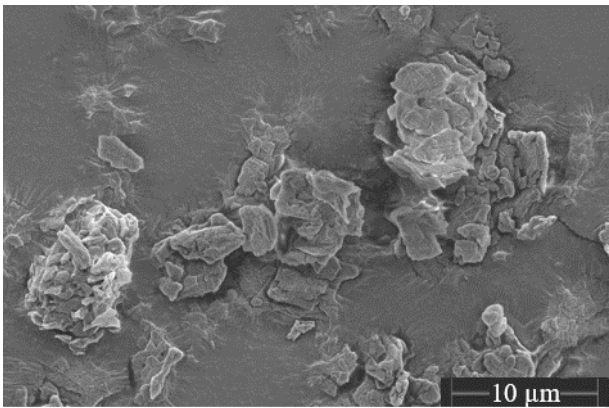
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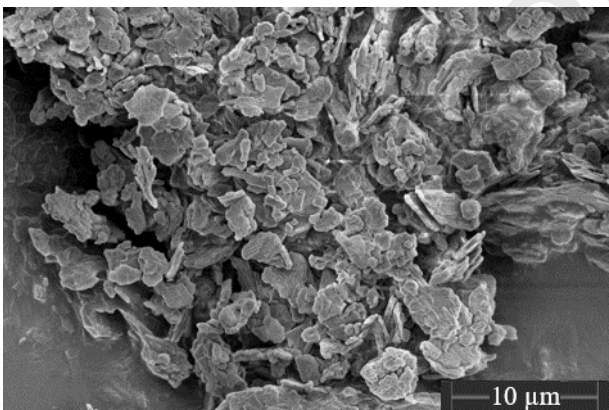
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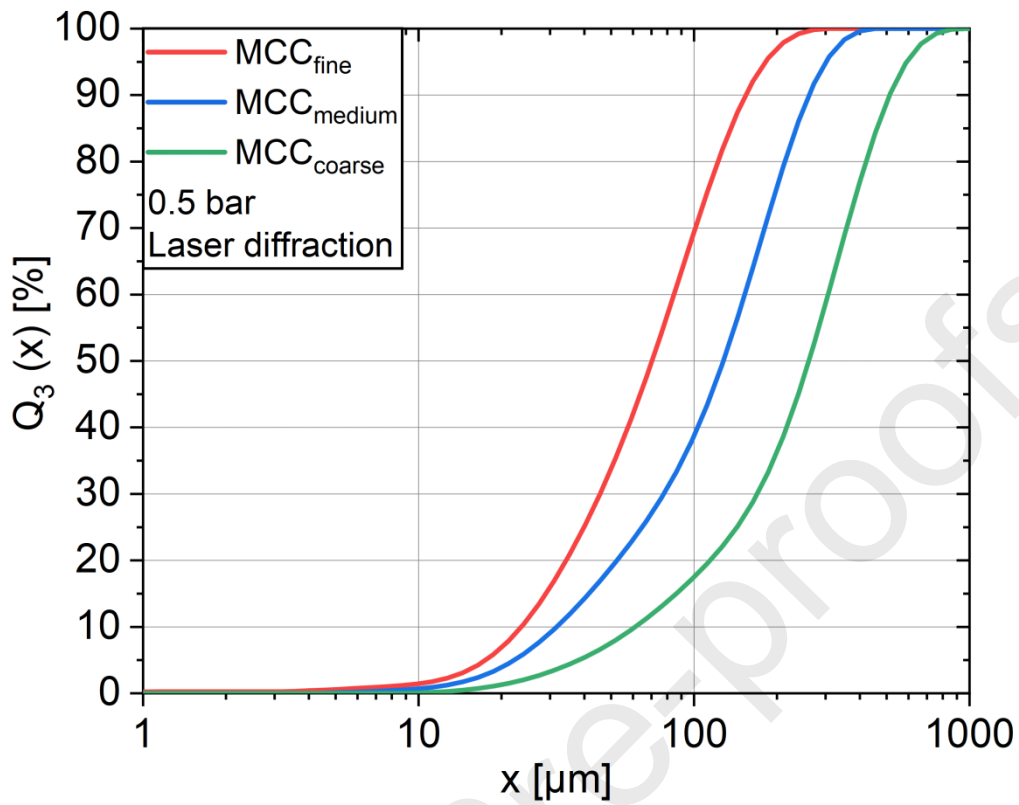
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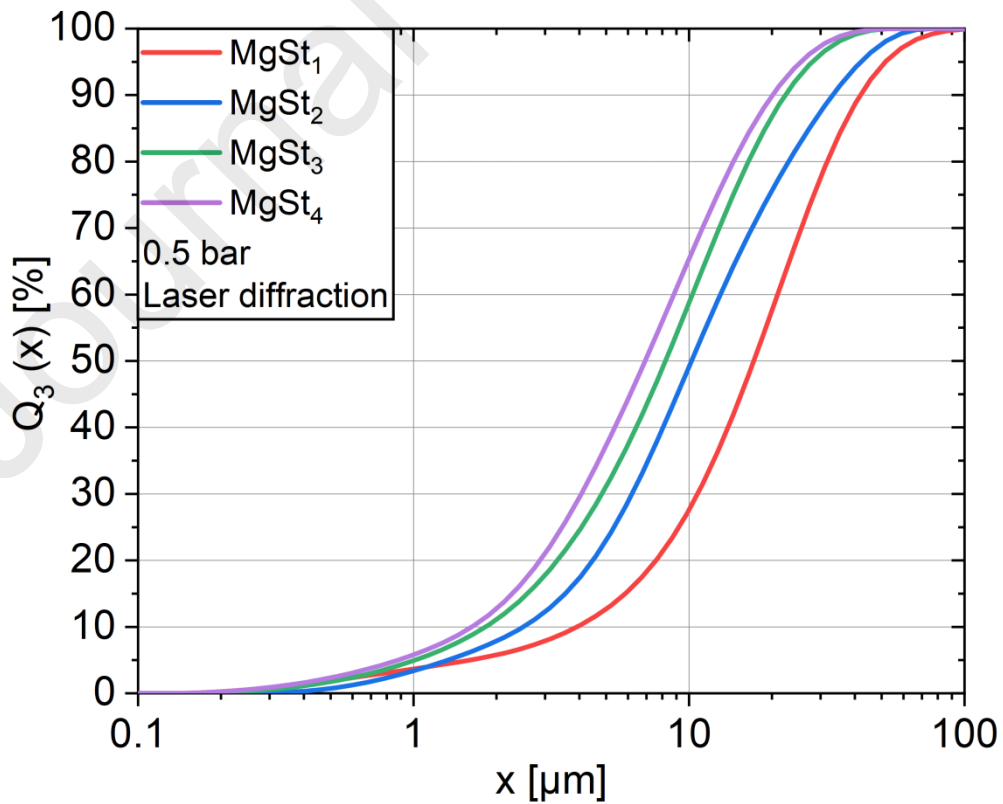
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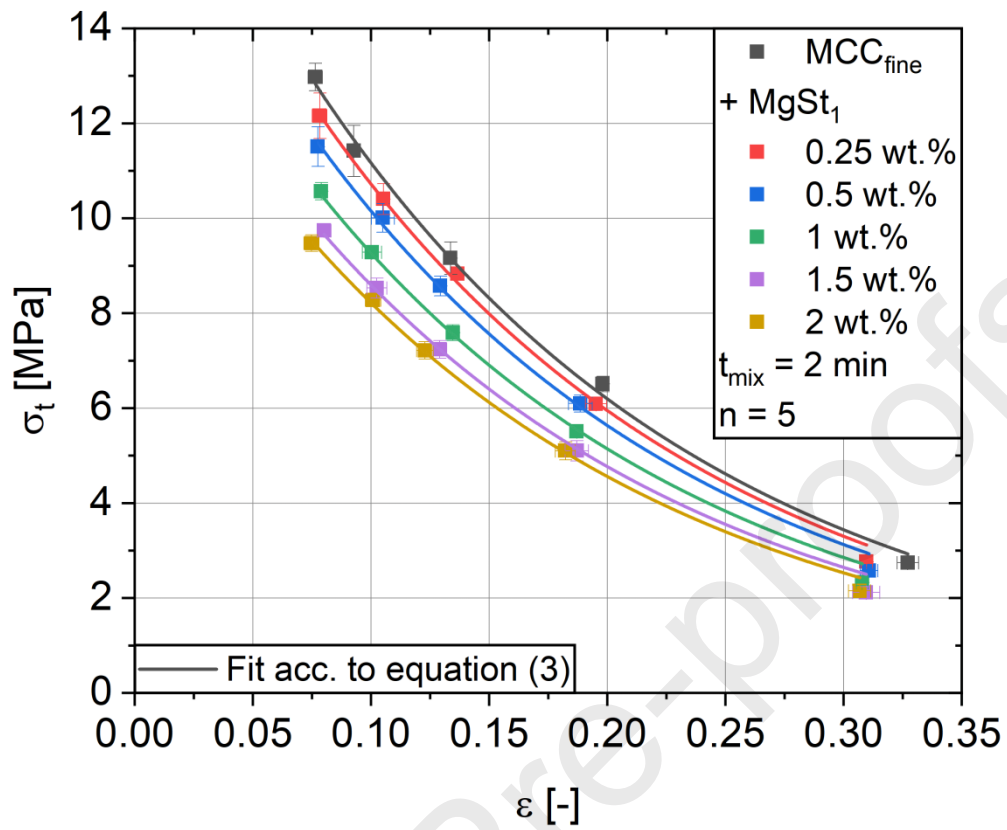
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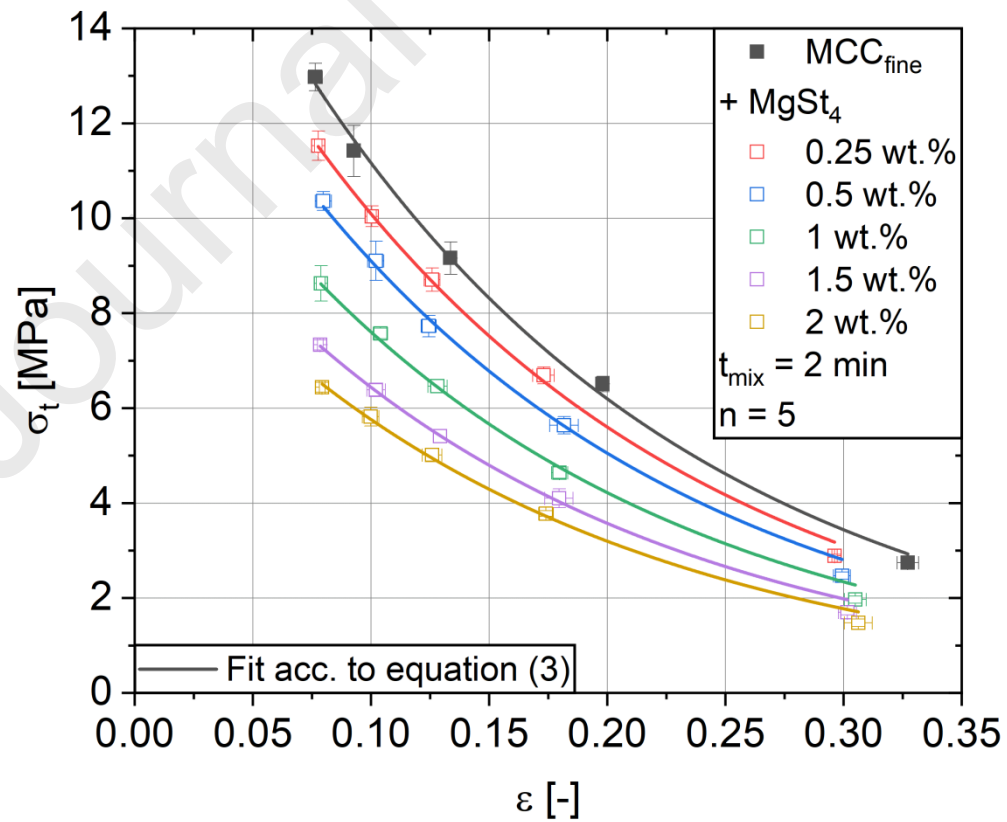
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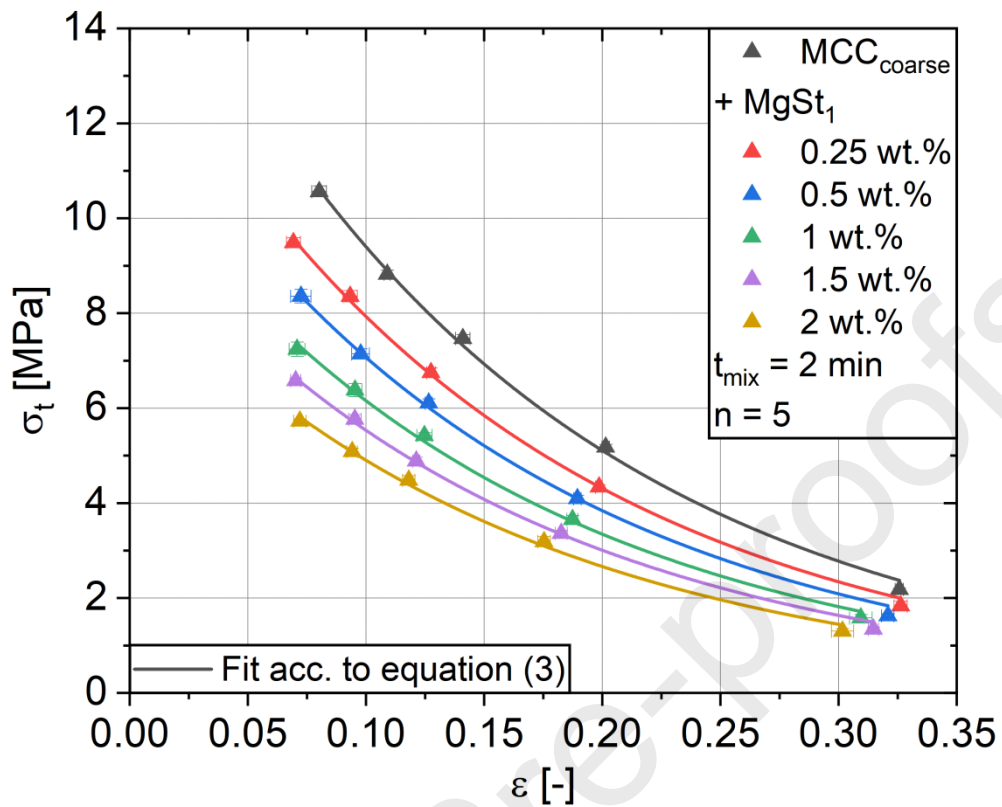
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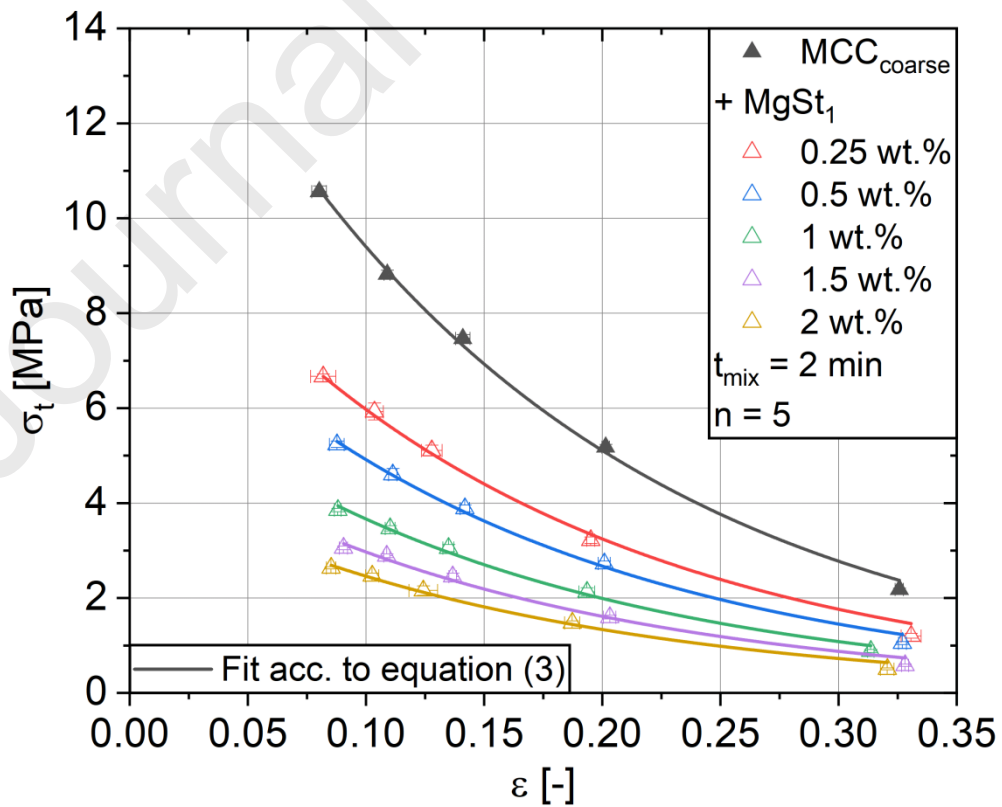
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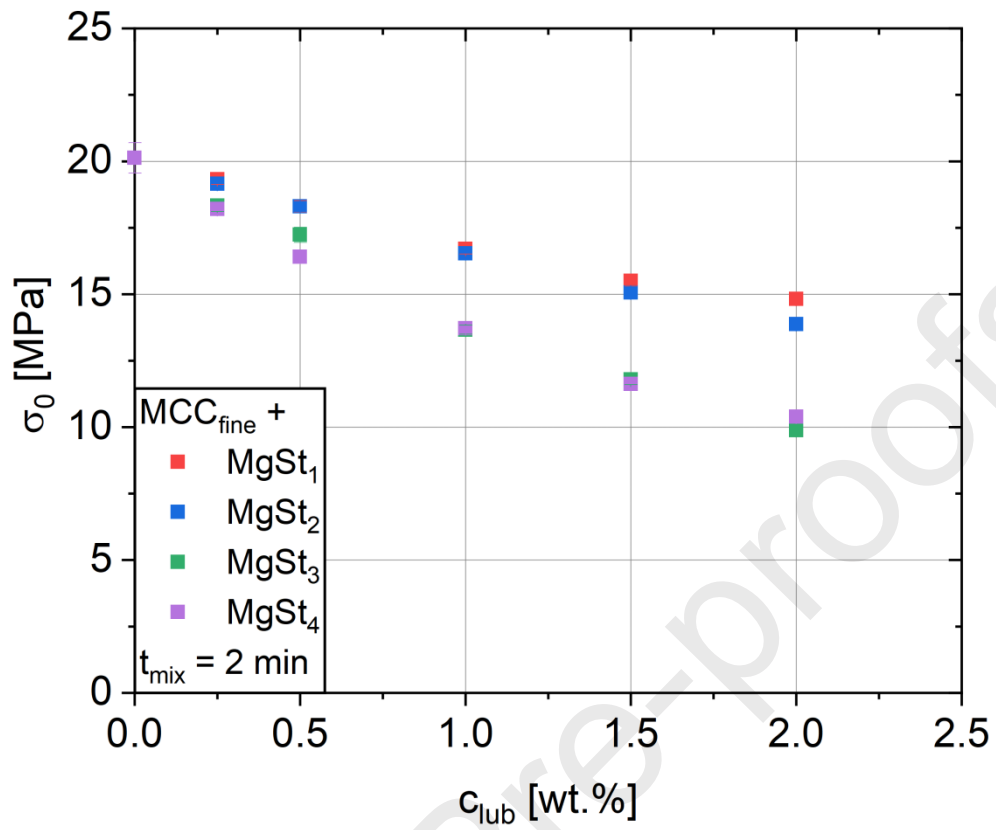
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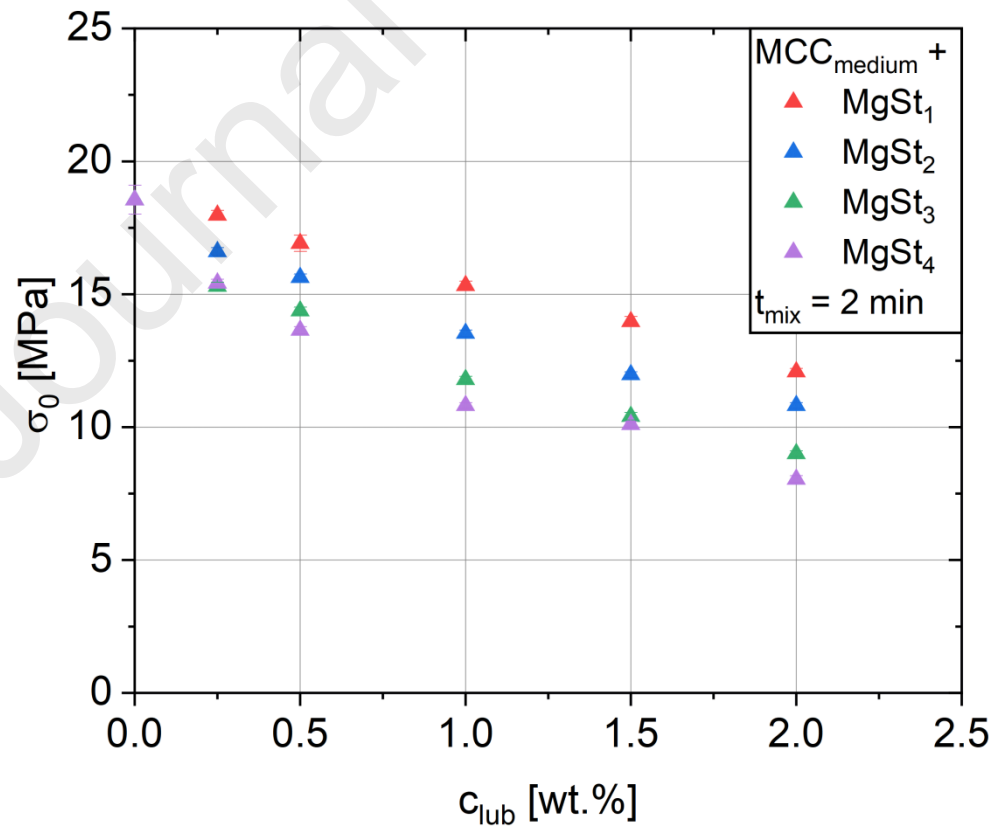
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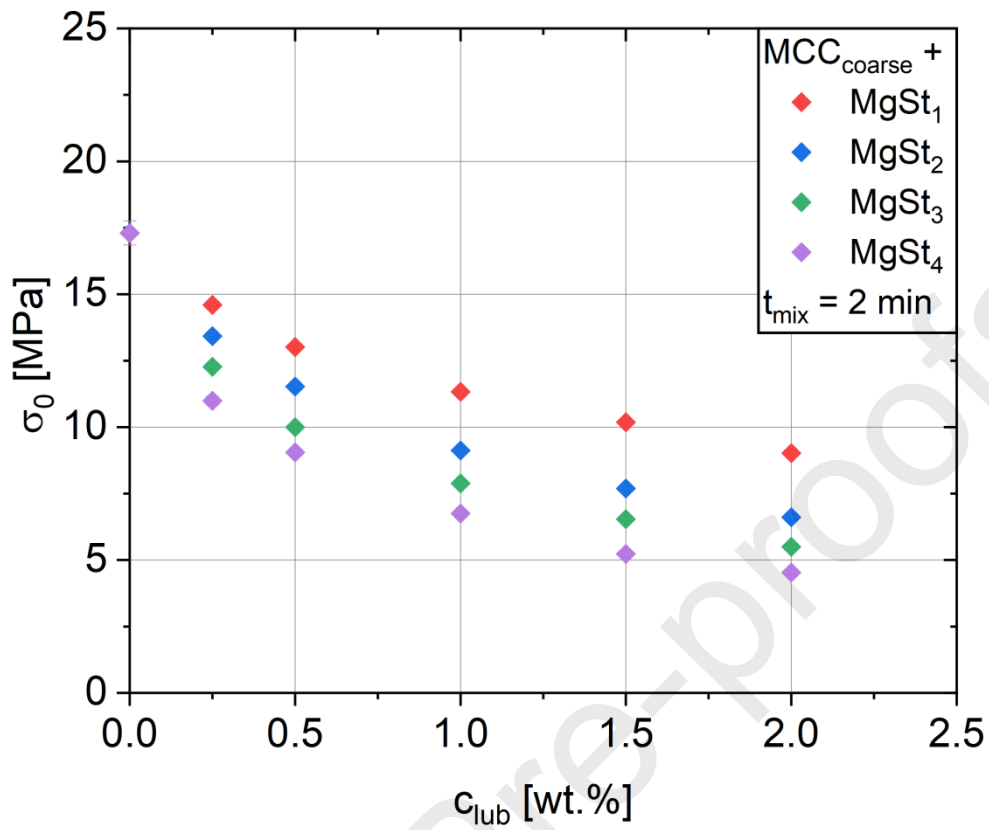
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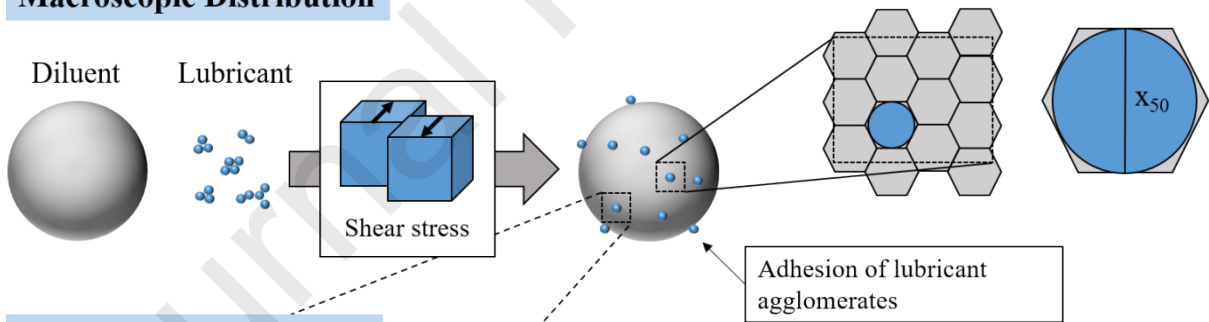


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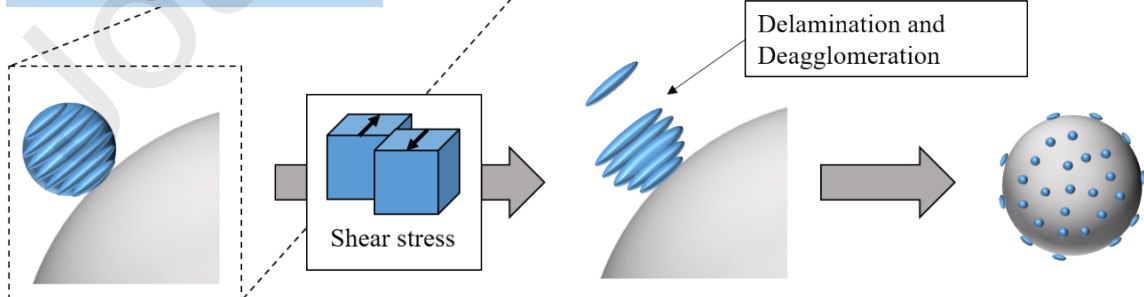


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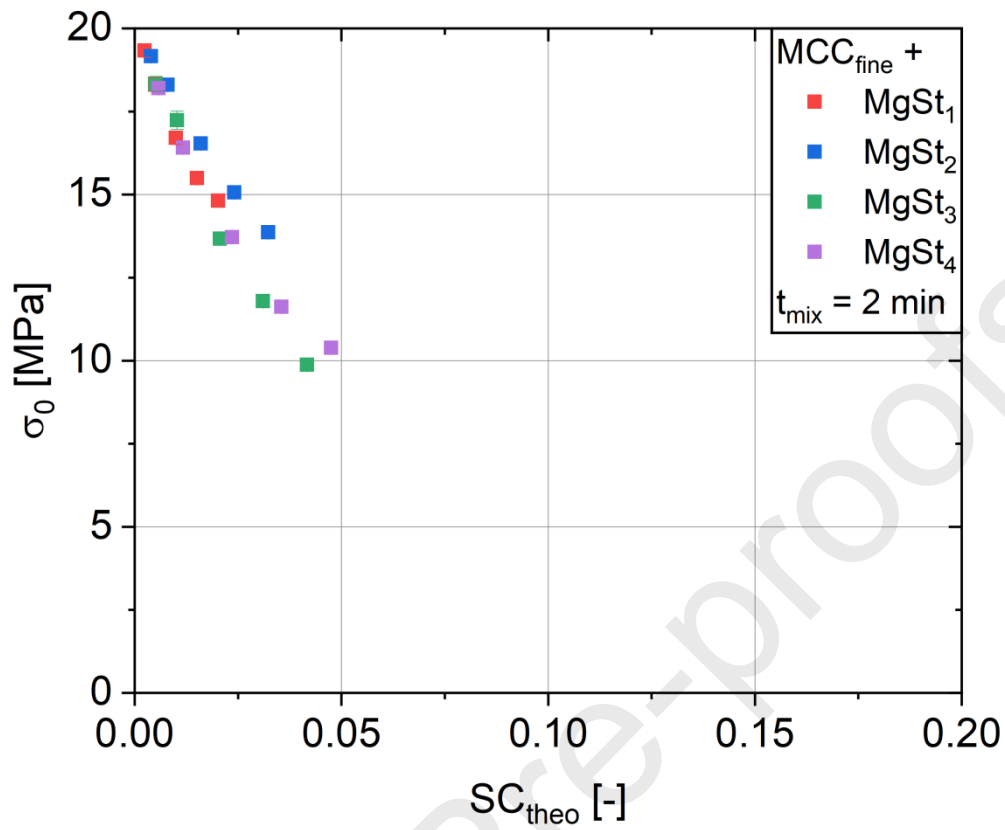
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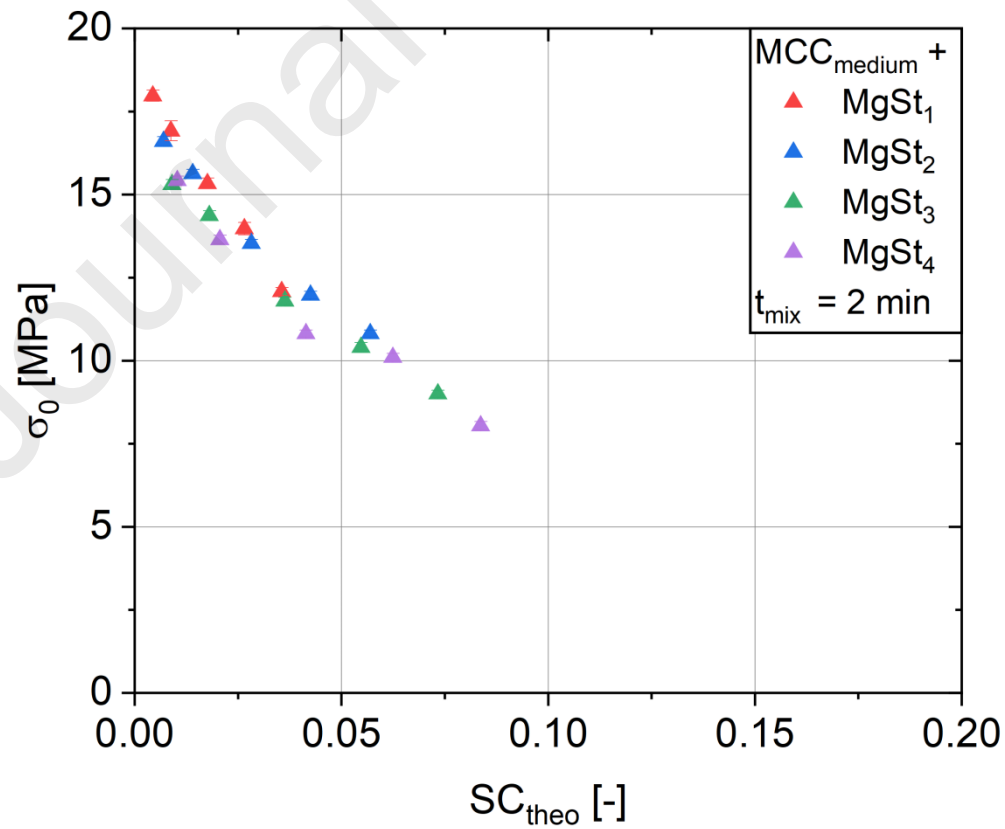
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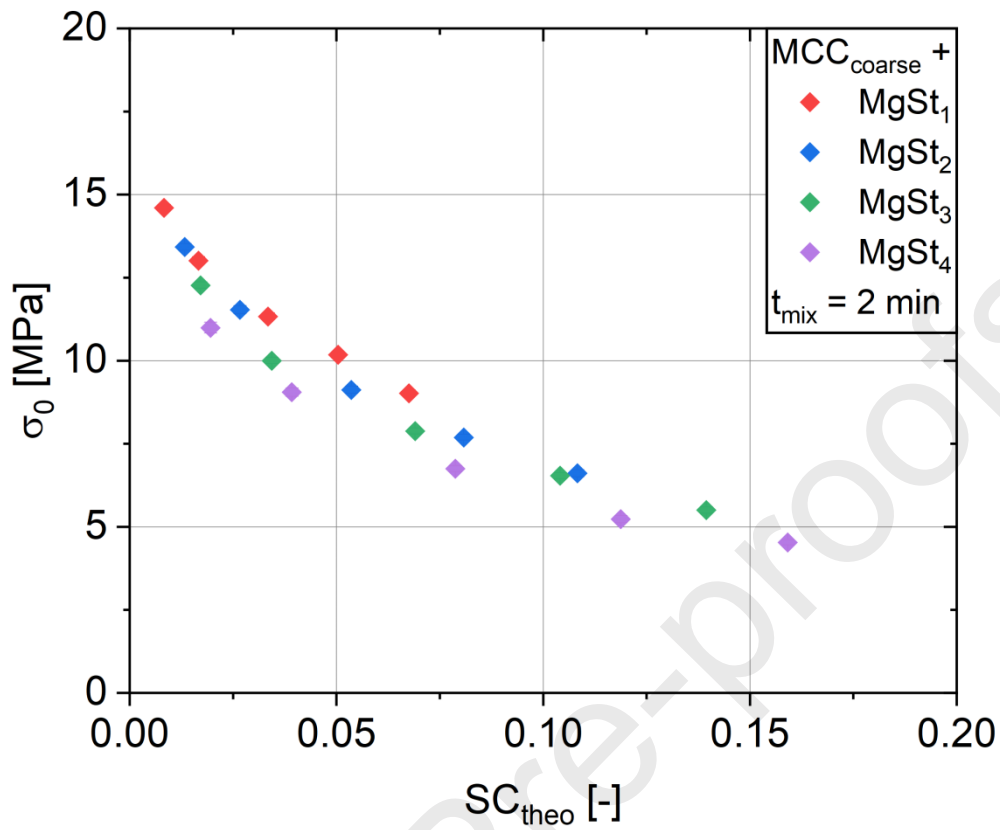
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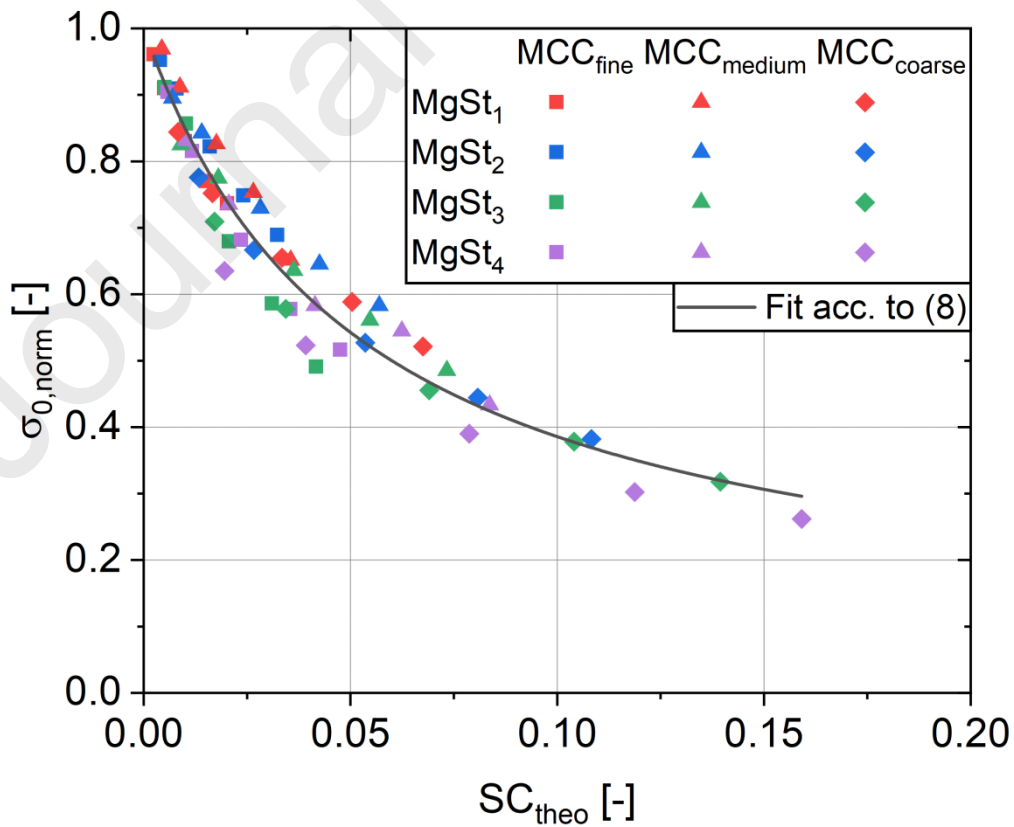
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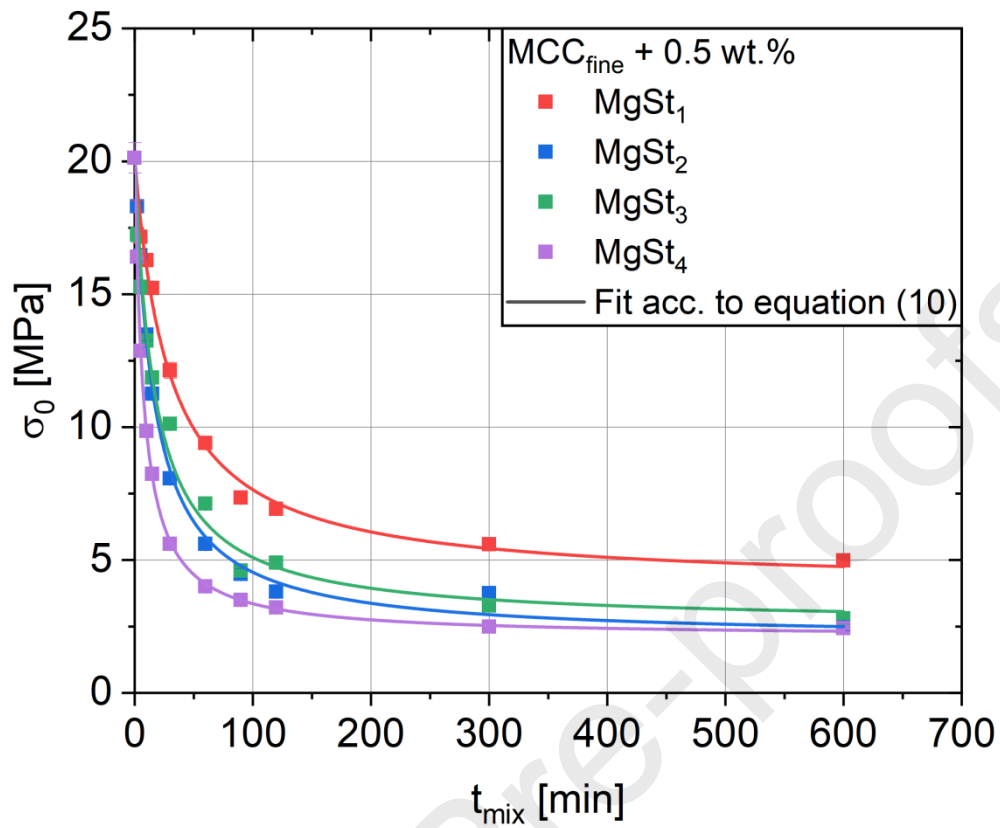
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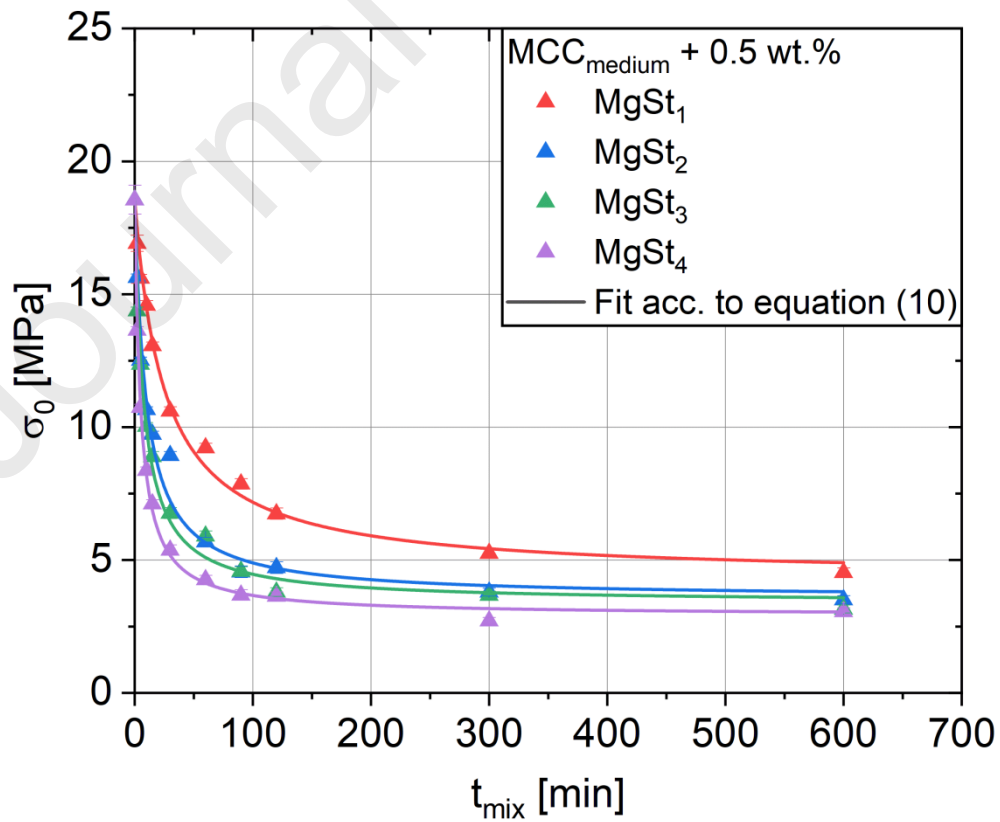
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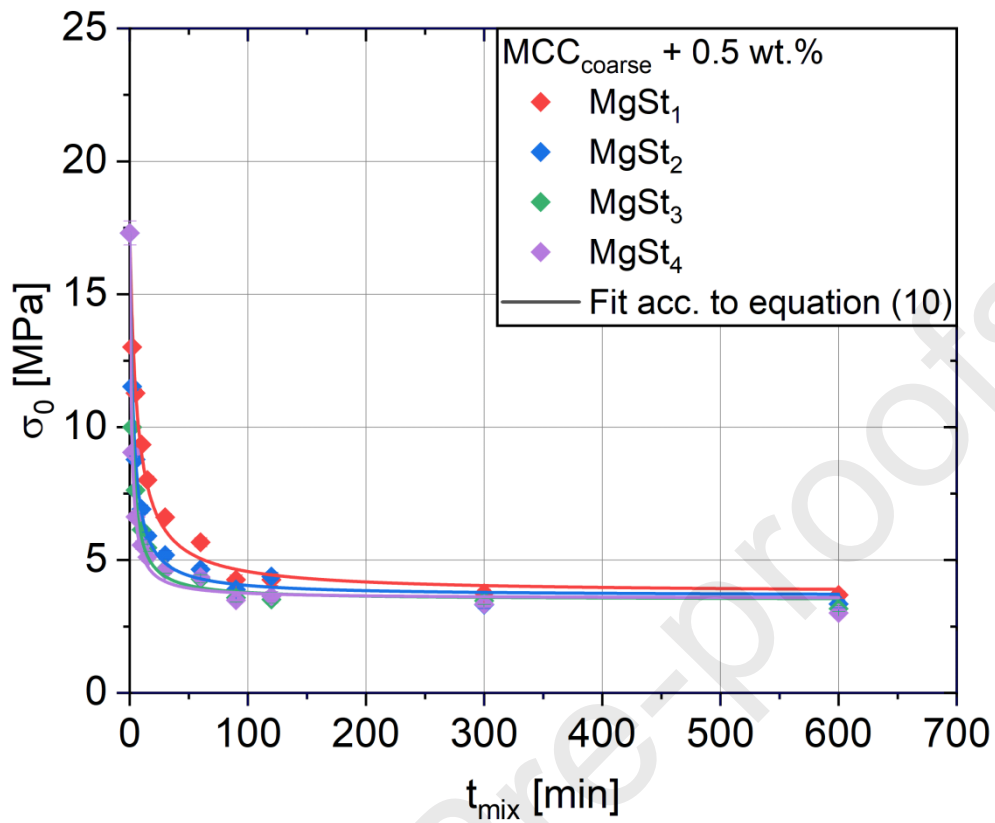
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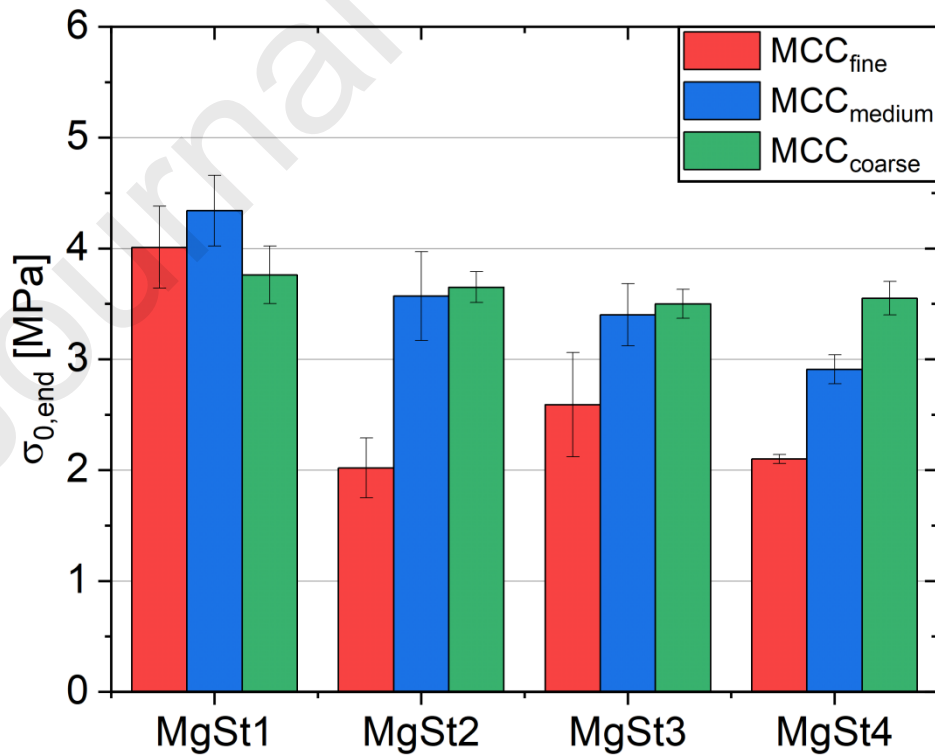
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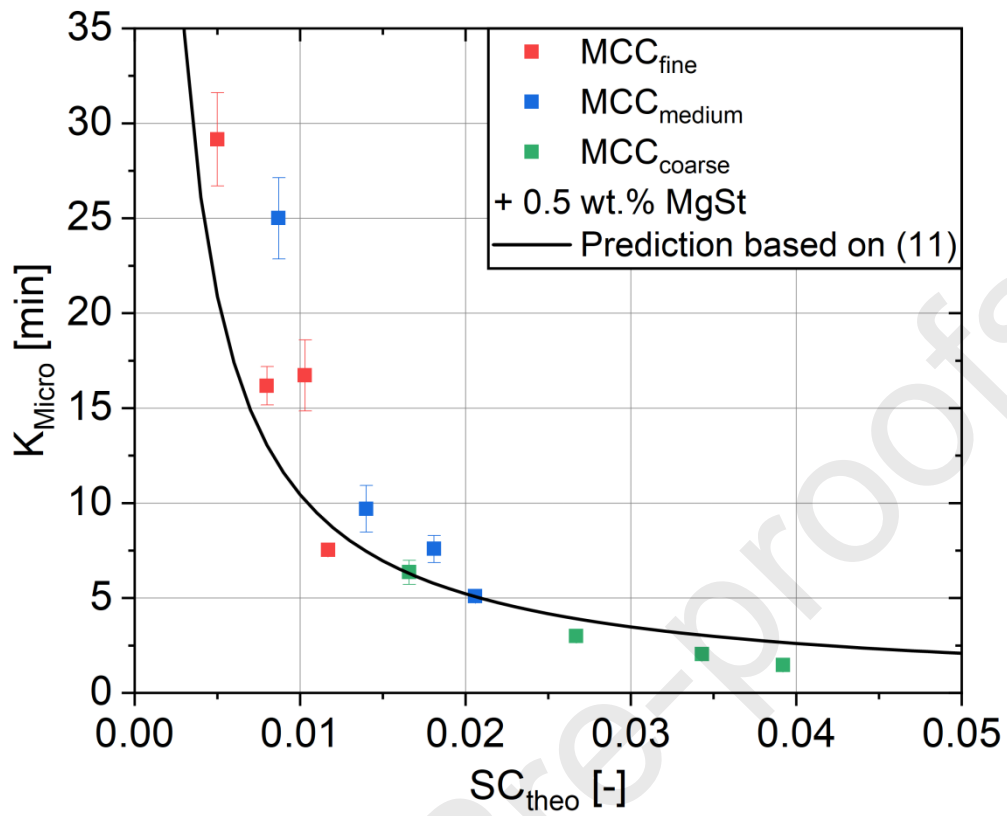
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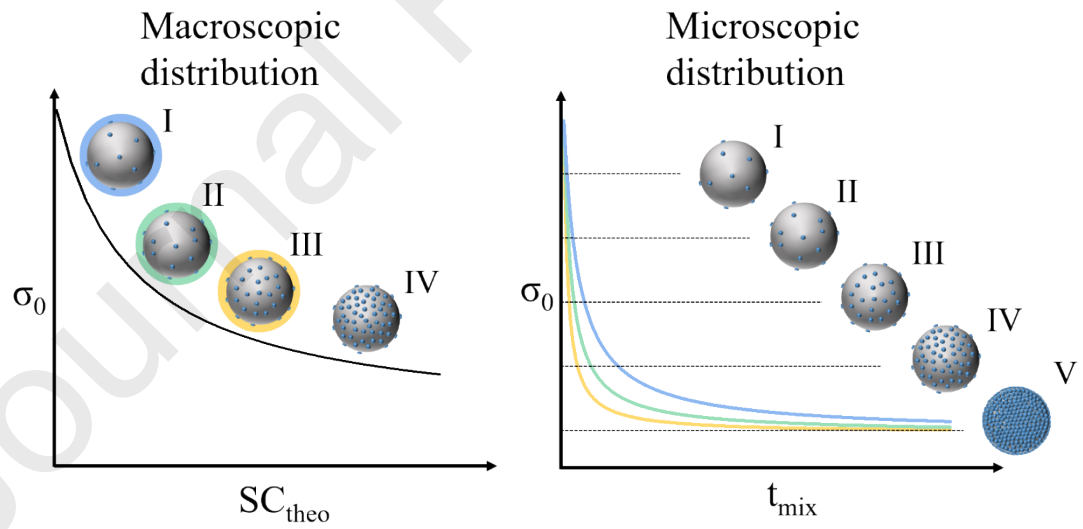
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